



“Seeing” Electric Network Frequency from Events

¹Lexuan Xu*, ²Guang Hua*, ¹Haijian Zhang†, ¹Lei Yu†, ³Ning Qiao

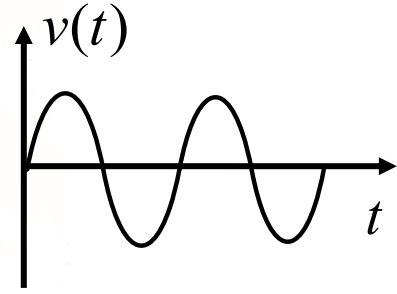
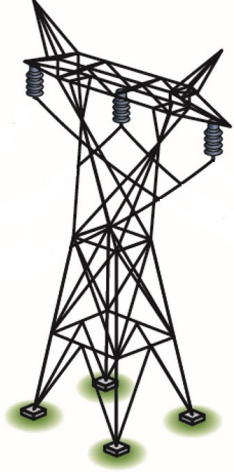
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(* *Equal contribution*, † *Corresponding author*)

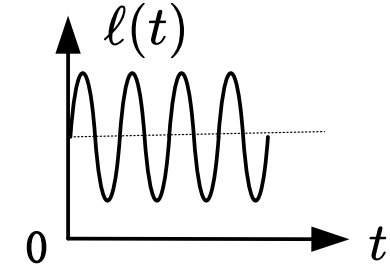
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Quick Review



Power Supply

Power to Illumination

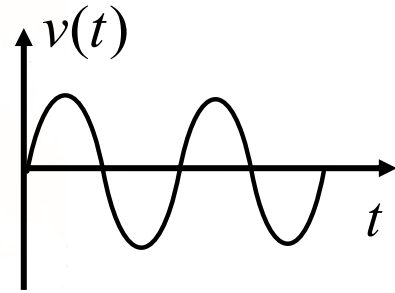
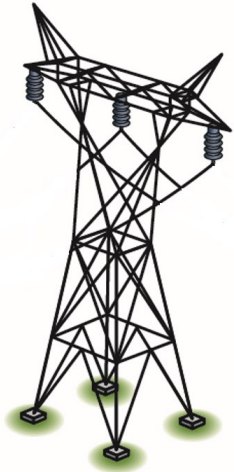


Light Flickering

Quick Review

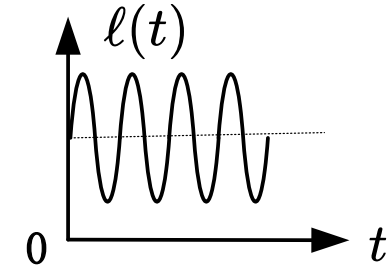
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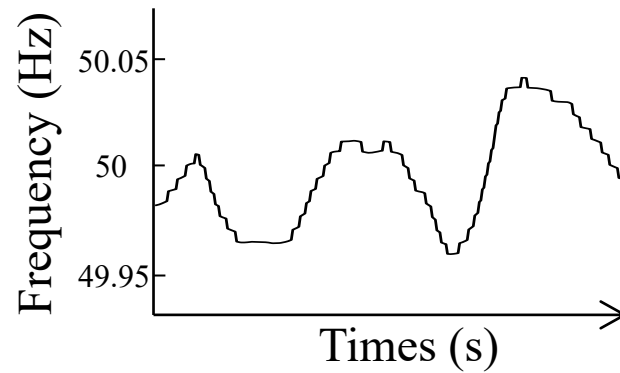
Power Supply

Power to Illumination



Light Flickering

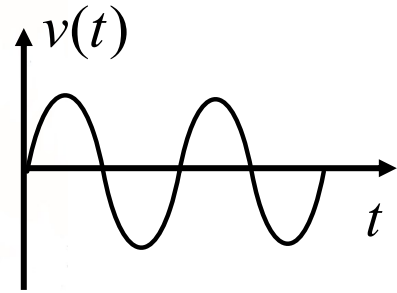
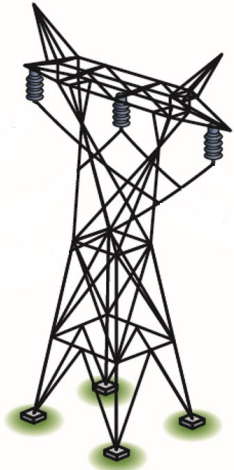
Transmission frequency



Electric Network Frequency (ENF):

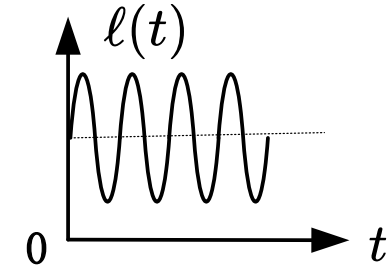
- Transmission frequency
- Fluctuates slightly
- Regional/Temporal variations

Quick Review

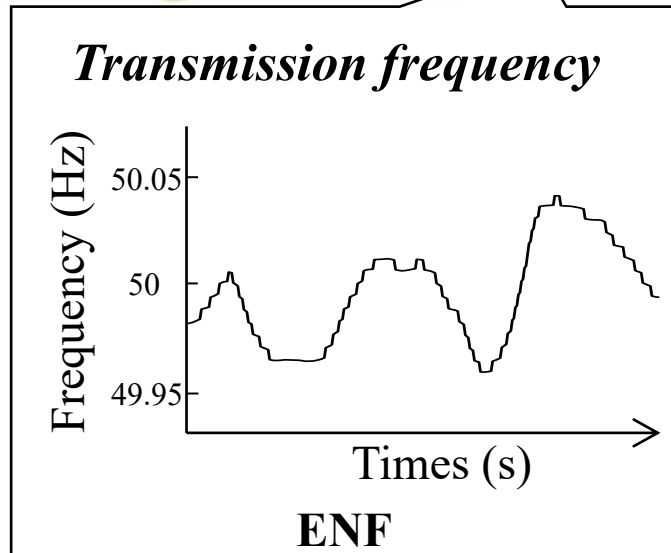


Power Supply

Power to Illumination

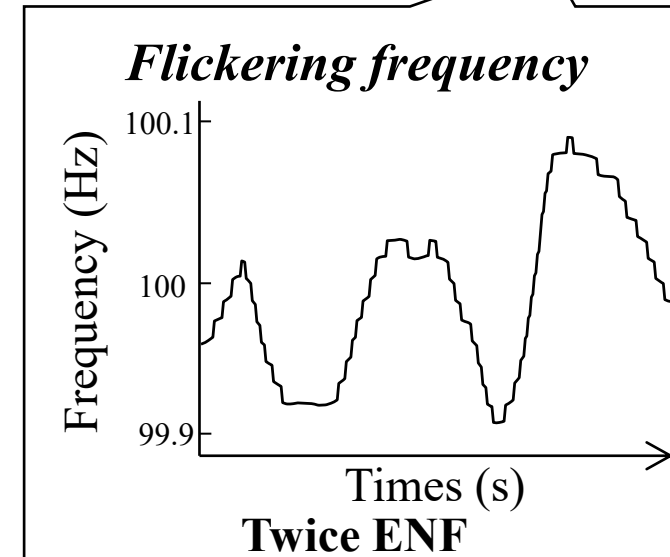


Light Flickering



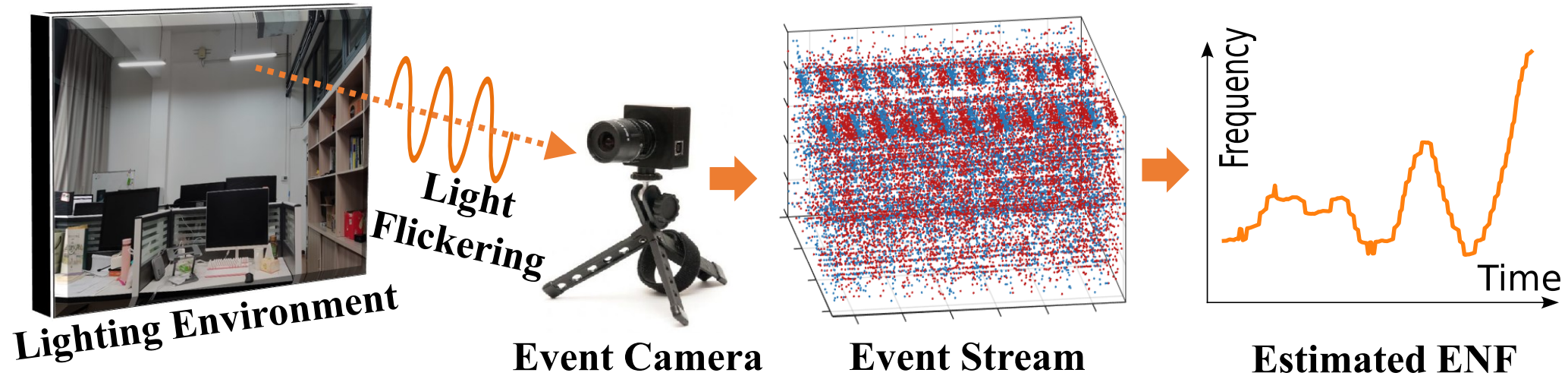
Electric Network Frequency (ENF):

- Transmission frequency
- Fluctuates slightly
- Regional/Temporal variations



Light Flickering:

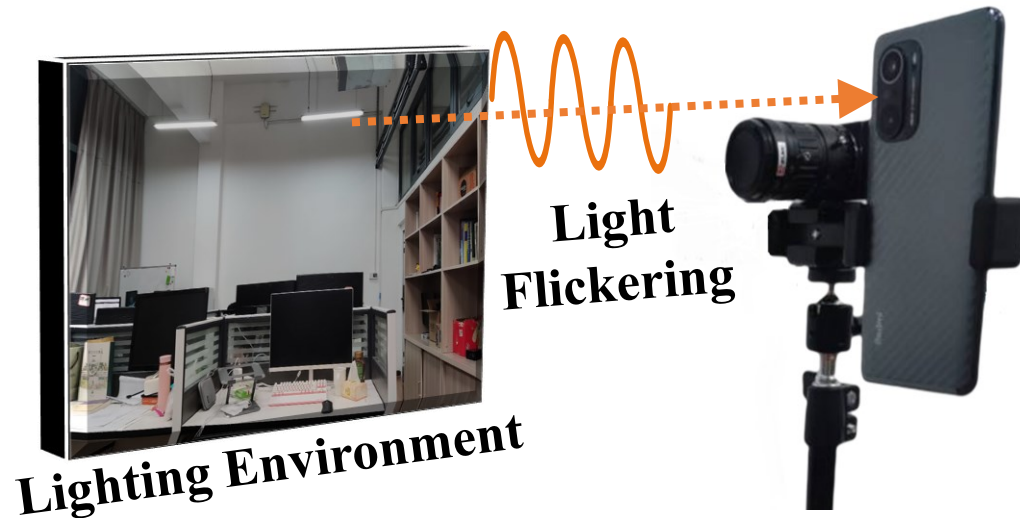
- *Twice ENF*



Contributions

- Validation of **ENF capture** in events.
- Introduction of pioneering event-based ENF extraction method (**E-ENF**).
- Construction of the first Event-Video hybrid ENF Dataset (**EV-ENFD**).

➤ Video-based ENF (V-ENF) extraction methods



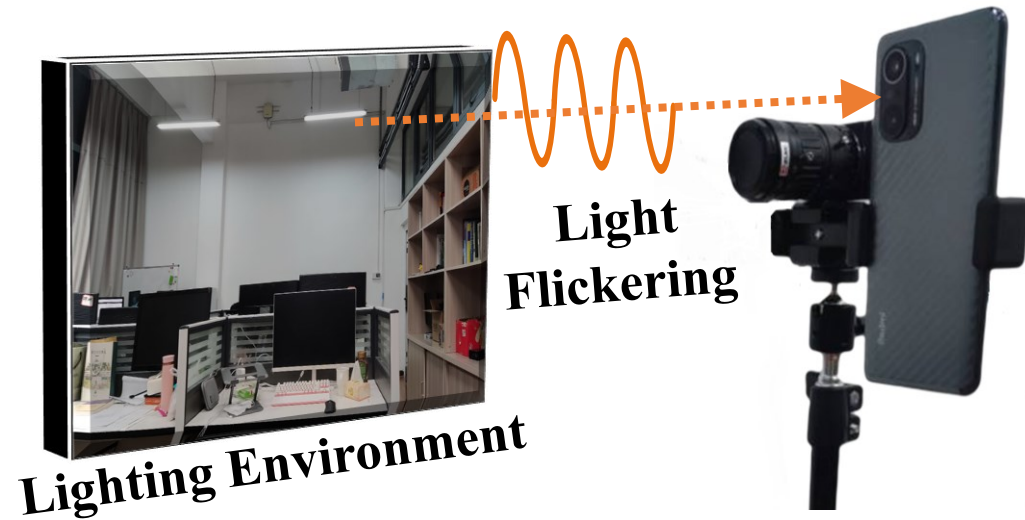
$$I(t) = G \{ \underset{\substack{\downarrow \\ \text{Signal}}}{l_{\text{ENF}}(t)} + \underset{\substack{\downarrow \\ \text{Noise}}}{l_{\text{M}}(t)} + \underset{\substack{\downarrow \\ \text{Noise}}}{l_{\text{S}}} + \underset{\substack{\downarrow \\ \text{Noise}}}{l_{\text{N}}(t)} \}$$

Averaging pixel intensity ➡ Light flickering



Brightness of the lighting

➤ Video-based ENF (V-ENF) extraction methods



Brightness of the lighting

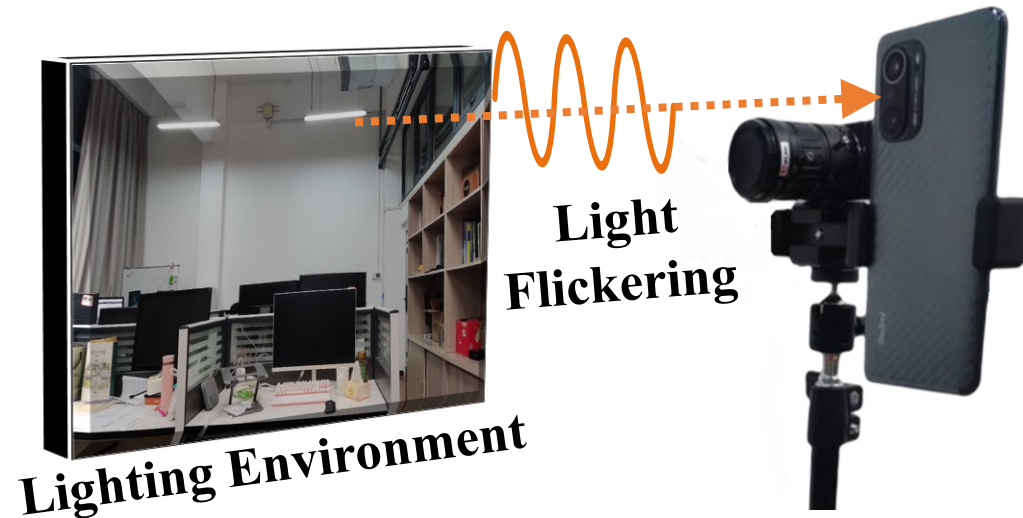
$$I(t) = G \{ \underset{\substack{\downarrow \\ \text{Signal}}}{l_{\text{ENF}}(t)} + \underset{\substack{\downarrow \\ \text{Noise}}}{l_{\text{M}}(t)} + \underset{\substack{\downarrow \\ \text{Noise}}}{l_{\text{S}}} + \underset{\substack{\downarrow \\ \text{Noise}}}{l_{\text{N}}(t)} \}$$

Averaging pixel intensity ➡ Light flickering

Challenges:

- Non-ideal sampling.
- Motion.
- Extreme lighting conditions.

➤ Video-based ENF (V-ENF) extraction methods



Brightness of the lighting

$$I(t) = G \{ \underset{\substack{\downarrow \\ \text{Signal}}}{l_{\text{ENF}}(t)} + \underset{\substack{\downarrow \\ \text{Noise}}}{l_{\text{M}}(t)} + \underset{\substack{\downarrow \\ \text{Noise}}}{l_{\text{S}}} + \underset{\substack{\downarrow \\ \text{Noise}}}{l_{\text{N}}(t)} \}$$

Averaging pixel intensity ➡ Light flickering

Challenges:

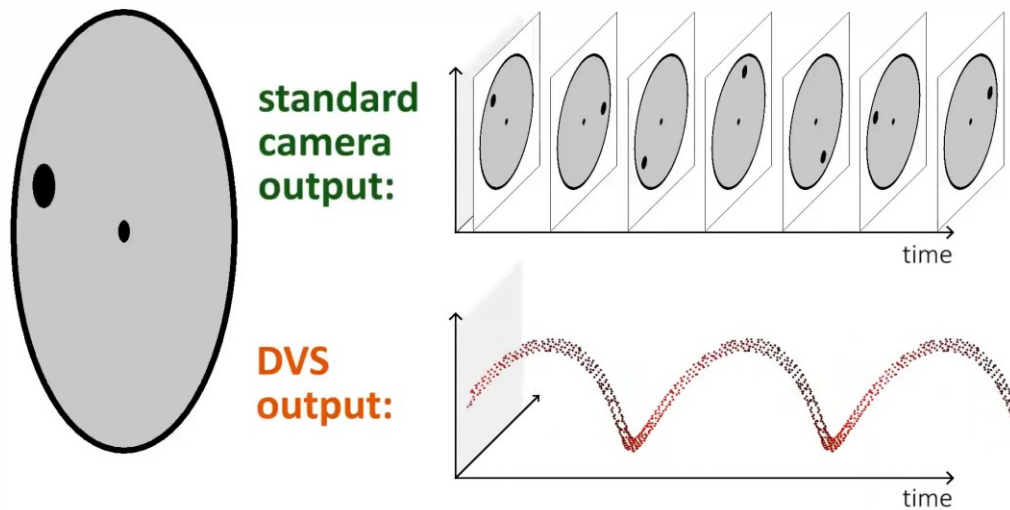
- Non-ideal sampling.
- Motion.
- Extreme lighting conditions.

Solved by
“Event Camera”

➤ Event Camera



– record pixel intensity changes
asynchronously per-pixel



● Event generation model:

$$\log(I(\mathbf{x}_k, t_k)) - \log(I(\mathbf{x}_k, t_k - \Delta t_k)) = p_k C$$

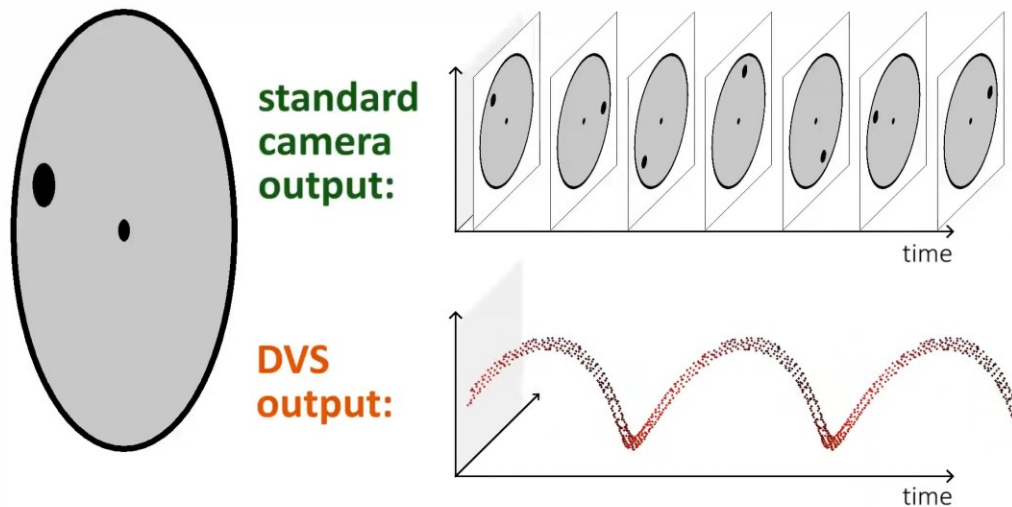
– Standard camera output and event camera output

(Video from here: <https://www.youtube.com/watch?v=LauQ6LWTkxM>)

➤ Event Camera



- record pixel intensity changes asynchronously per-pixel



- Event generation model:

$$\log(I(\mathbf{x}_k, t_k)) - \log(I(\mathbf{x}_k, t_k - \Delta t_k)) = p_k C$$

Advantages:

- High temporal resolution
- High dynamic range
- Low latency

- Standard camera output and event camera output

(Video from here: <https://www.youtube.com/watch?v=LauQ6LWTkxM>)

- Pixel intensity under ideal flickering:

$$I_x(t) = A(t) \cos(4\pi f_e(t) + \phi) + B(t)$$

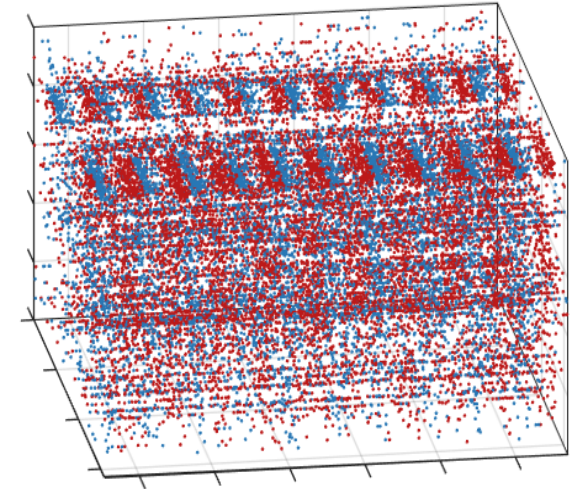
- Event generation model:

$$\text{Let } p \triangleq (B(t) + \sqrt{B(t)^2 - A(t)^2}) / 2, \quad q \triangleq (B(t) - \sqrt{B(t)^2 - A(t)^2}) / A(t)$$

$$\text{ENF Capture} \quad \log(I_x(t)) = \log p + 2 \sum_m (-1)^{m-1} \frac{q^m}{m} \cos m\omega$$

$$\text{Illumination Events} \quad \log(I_x(t_k)) - \log(I_x(t_k - \Delta t_k)) = pC$$

Event Stream



- Pixel intensity under ideal flickering:

$$I_x(t) = A(t) \cos(4\pi f_e(t) + \phi) + B(t)$$

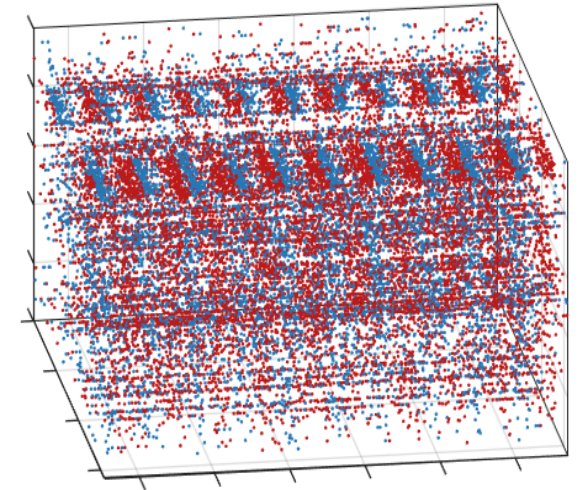
- Event generation model:

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$$\text{Illumination Events} \quad \log(I_x(t_k)) - \log(I_x(t_k - \Delta t_k)) = pC$$

Event Stream



Conclusions:

- In addition to twice the ENF, its **harmonic content** was also recorded in the event stream.
- Light flickering generates numerous events exhibiting a unified polarity simultaneously, unlike those from noise and motion.

Event-based ENF (E-ENF)

Temporal Sampling

Spatial Sampling

Harmonic Selection

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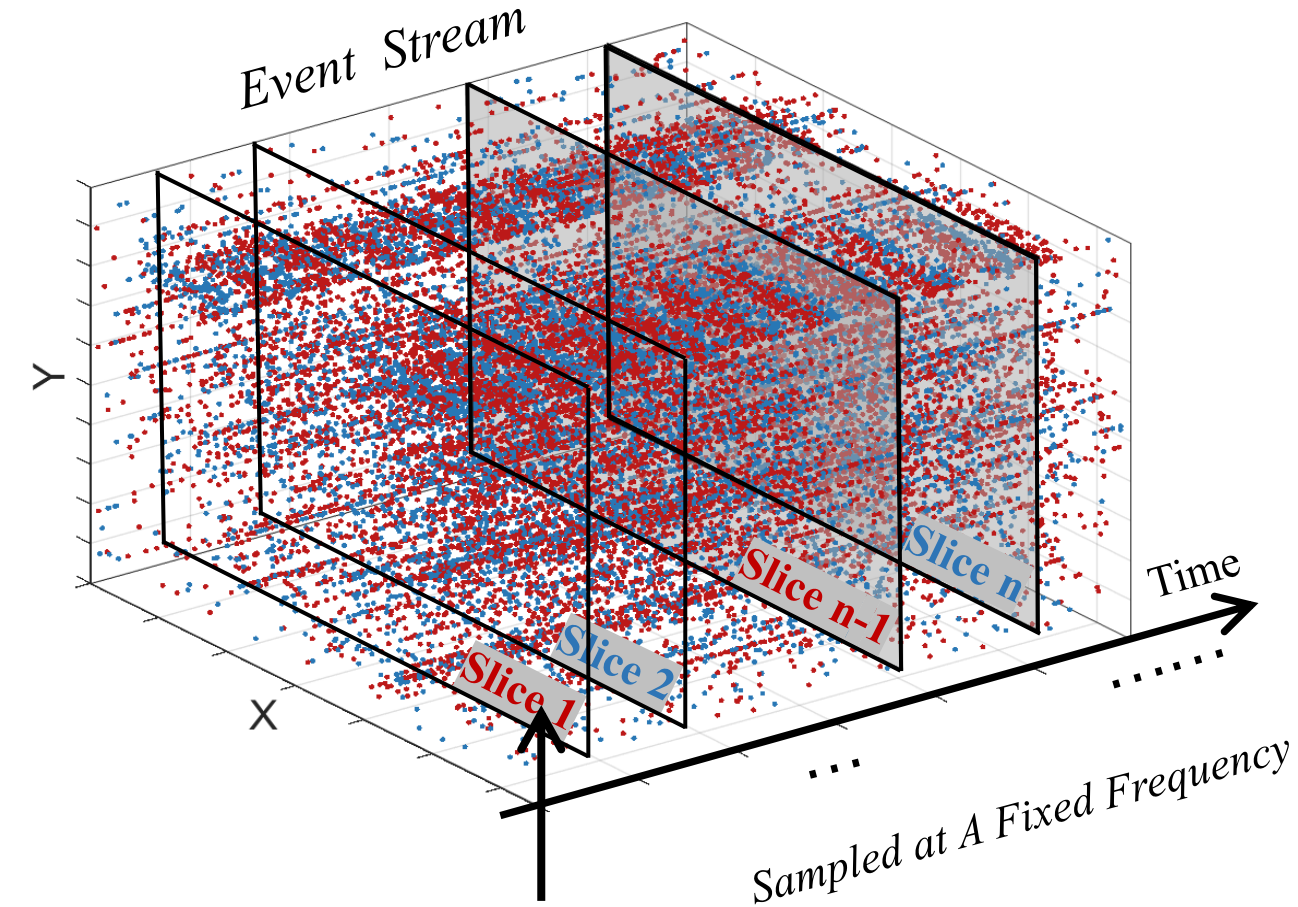
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➤ Temporal Sampling

● Event Stream



Event Slices



- Frame the asynchronous events into uniform time intervals

Event-based ENF (E-ENF)

Temporal Sampling

Spatial Sampling

Harmonic Selection

JUNE 18-22, 2023

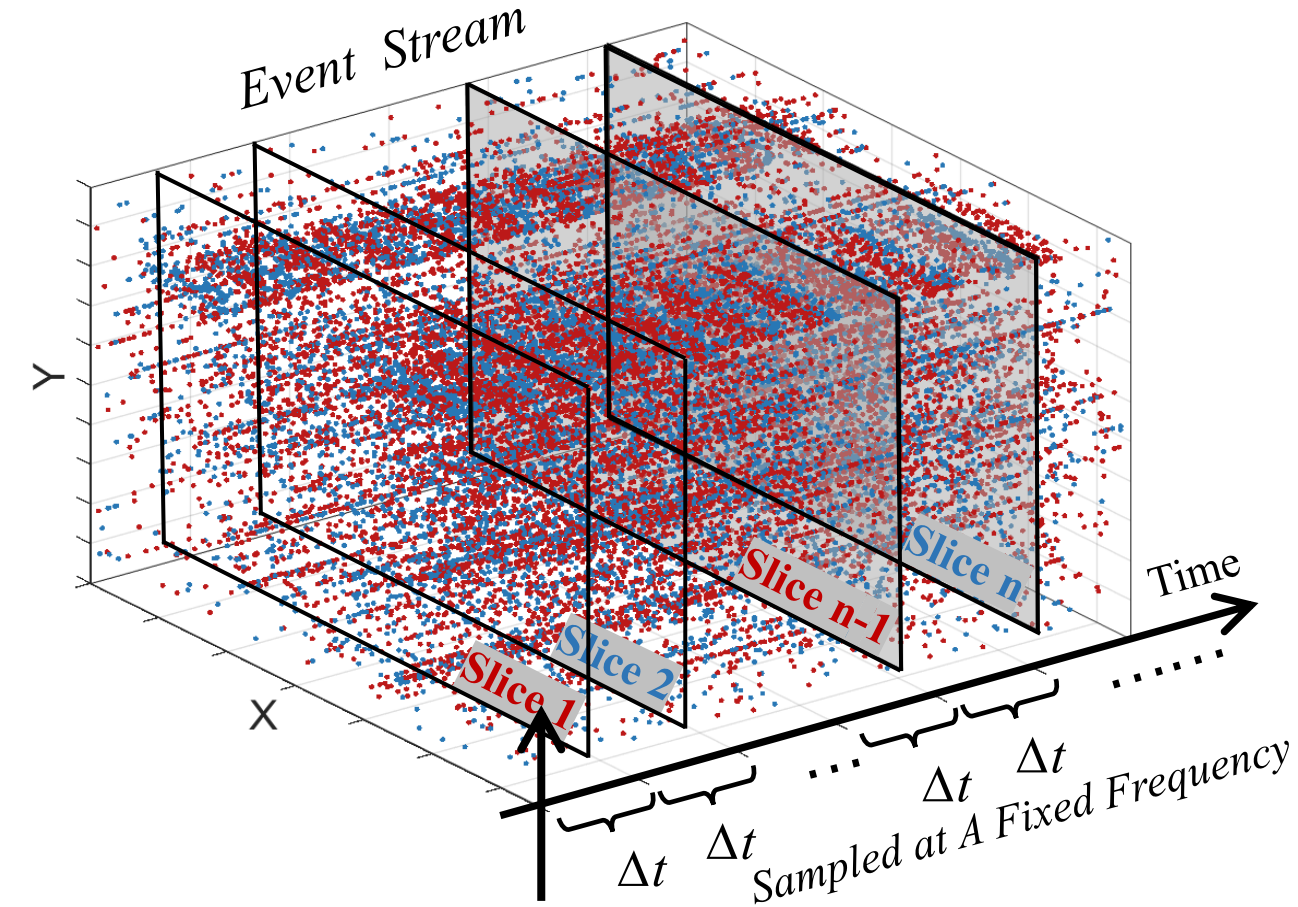
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➤ Temporal Sampling

● Event Stream



Event Slices



- Frame the asynchronous events into uniform time intervals

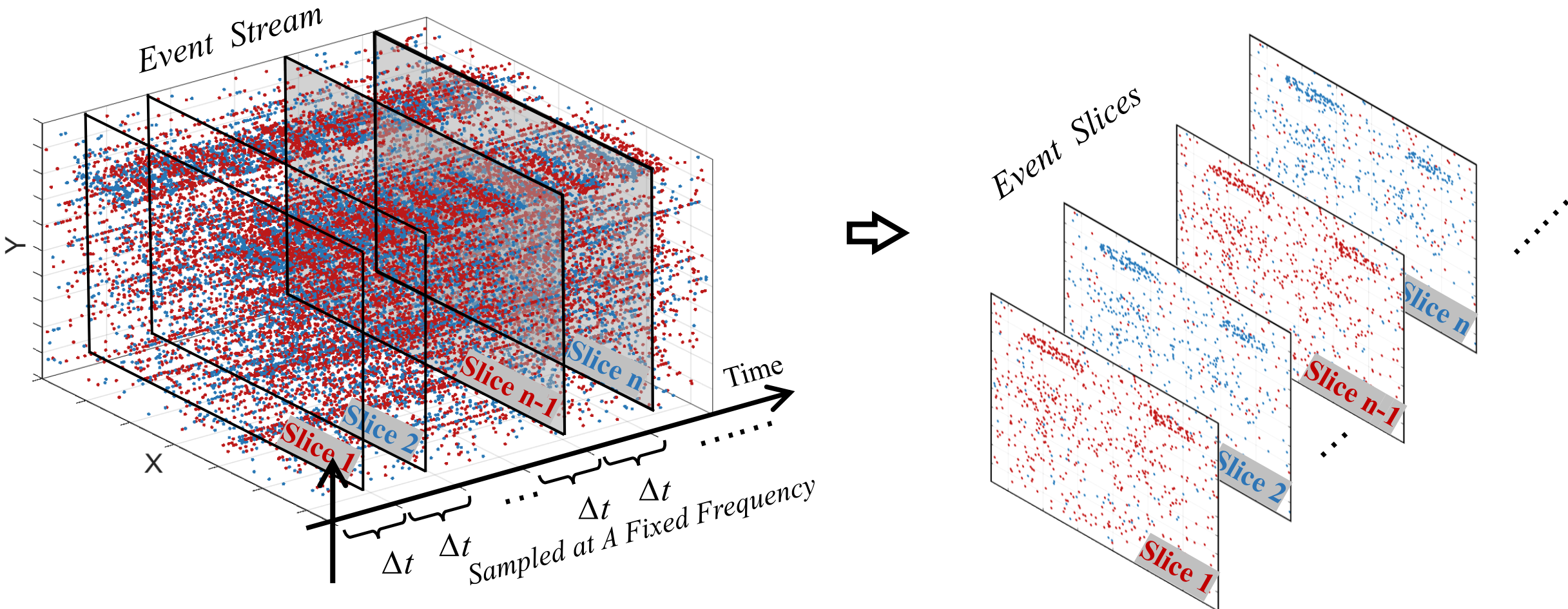
Event-based ENF (E-ENF)

Temporal Sampling

Spatial Sampling

Harmonic Selection

➤ Temporal Sampling



- Frame the asynchronous events into uniform time intervals

Event-based ENF (E-ENF)

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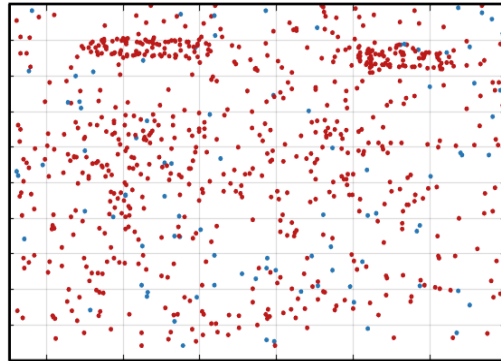
➤ Spatial Sampling

● Event Slices

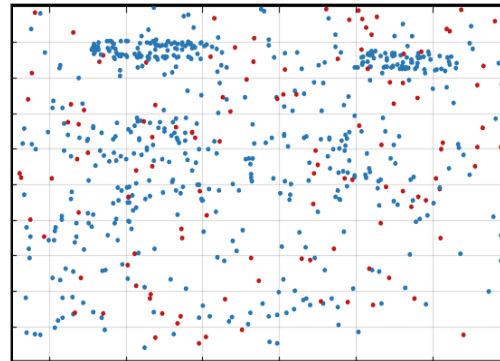


Polar Sequence

Slice n-1



Slice n



Event Slices

- Inconsistent polarity
- Inconsistent location



- Judge flickering from inconsistent polarity and location

Event-based ENF (E-ENF)

Temporal Sampling

Spatial Sampling

Harmonic Selection

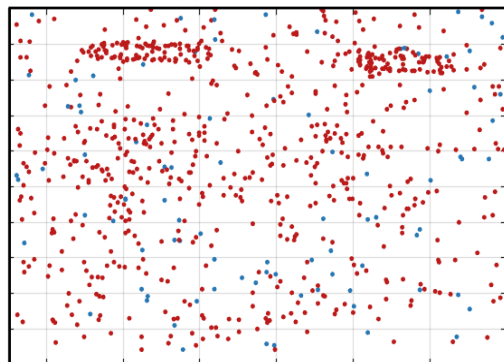
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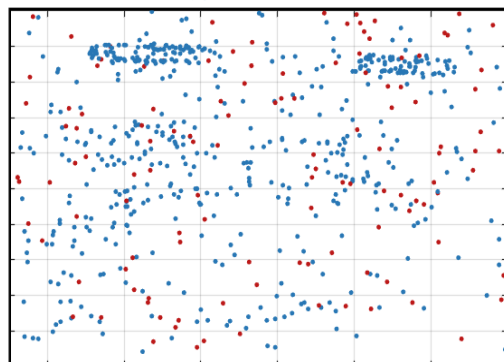
➤ Spatial Sampling

● Event Slices ➡ Polar Sequence

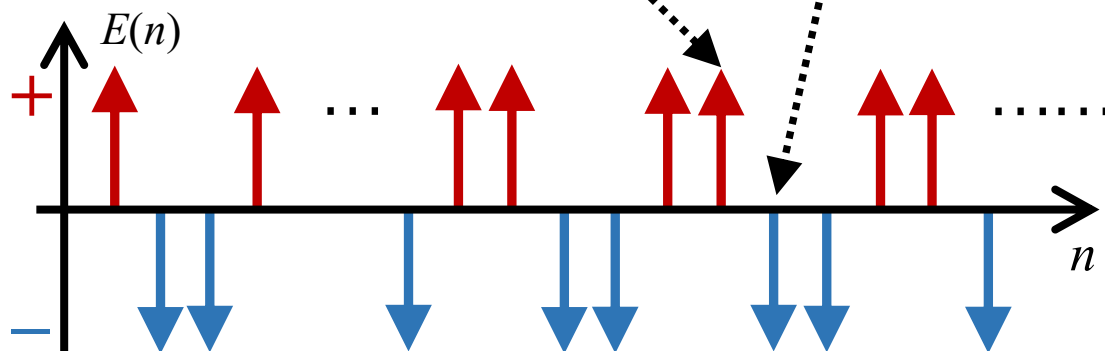
Slice n-1



Slice n



Convert All Spatial Event Polarities to A Single Polarity



Event Slices

- Inconsistent polarity
- Inconsistent location



Polar Sequence $E(n)$

- One-dimensional
- Contains only ± 1
- Encodes illumination changes

- Judge flickering from inconsistent polarity and location

Event-based ENF (E-ENF)

Temporal Sampling

Spatial Sampling

Harmonic Selection

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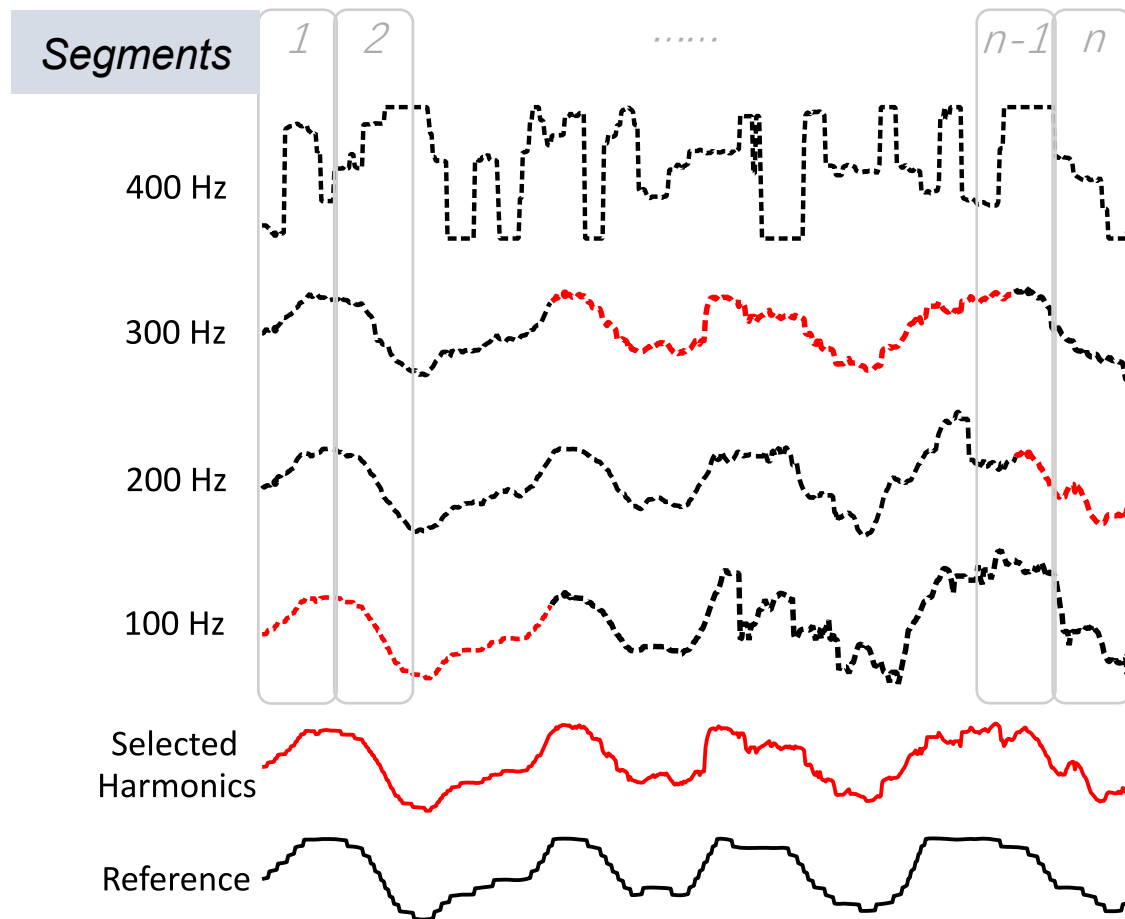


➤ Harmonic Selection

● Polar Sequence



ENF Estimation



● Polar Sequence $E(n)$

- Combine the time-frequency variation into ENF estimation

Event-based ENF (E-ENF)

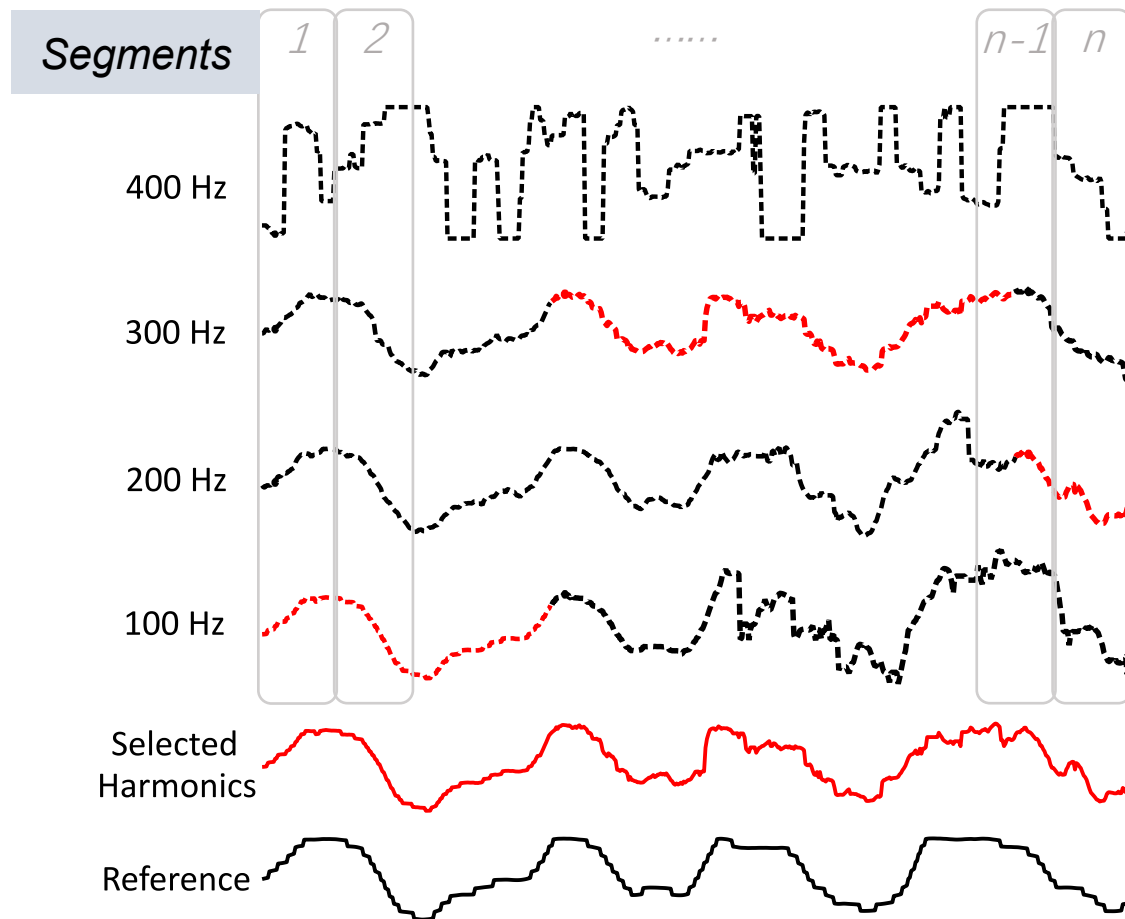
Temporal Sampling

Spatial Sampling

Harmonic Selection

➤ Harmonic Selection

● Polar Sequence ➡ ENF Estimation



● Polar Sequence $E(n)$



● STFT and peak search

- Combine the time-frequency variation into ENF estimation

Event-based ENF (E-ENF)

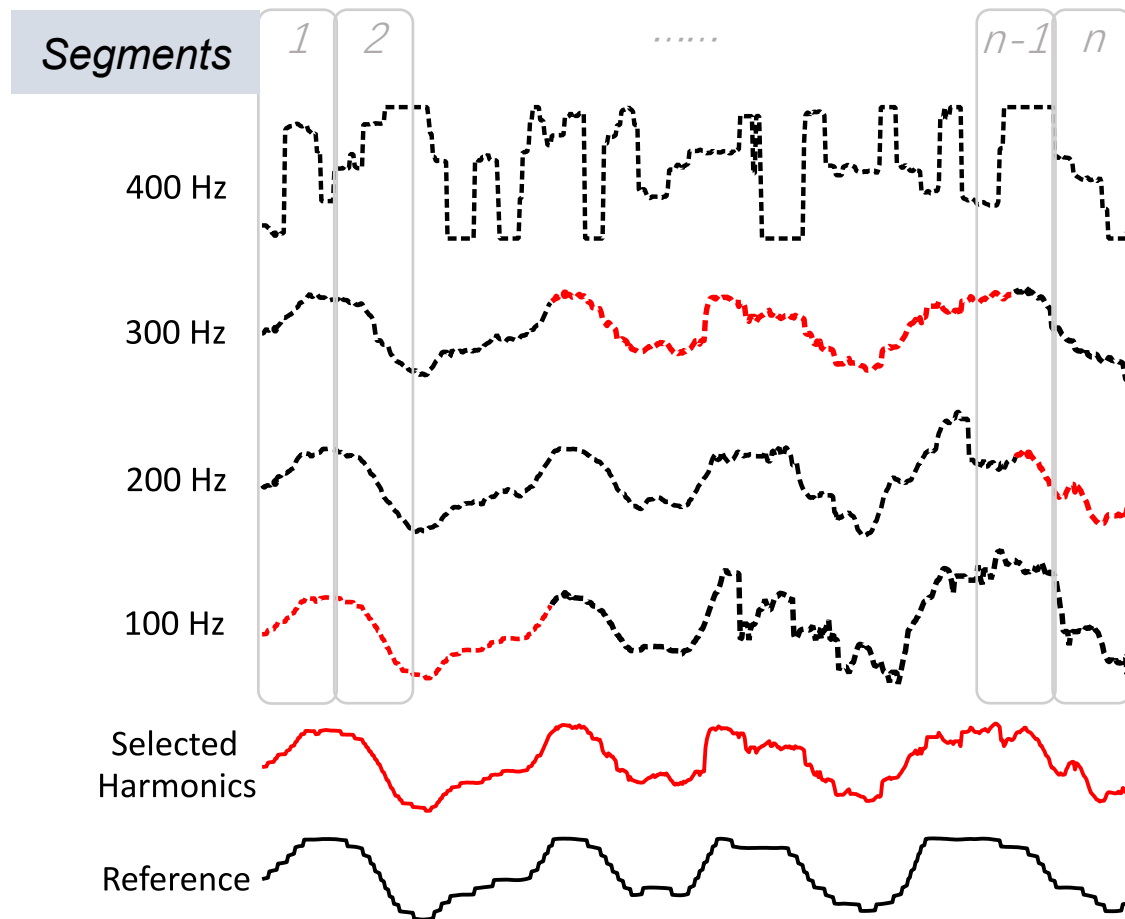
Temporal Sampling

Spatial Sampling

Harmonic Selection

➤ Harmonic Selection

● Polar Sequence ➡ ENF Estimation



● Polar Sequence $E(n)$



● STFT and peak search



● Harmonic Selection

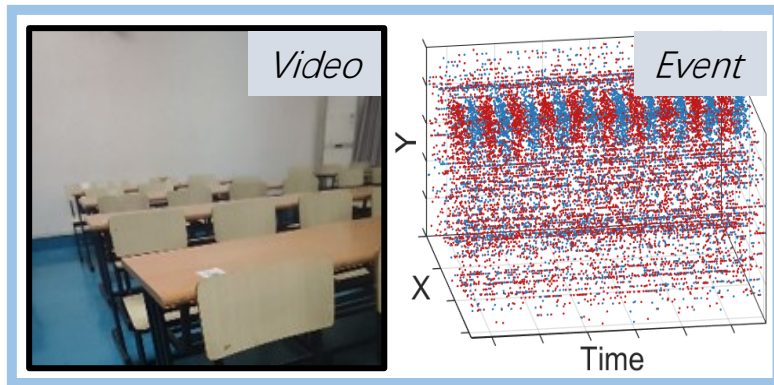
✓ Selection Criteria : $S_m = \sum_{n=1}^{N_f} |f_m[n] - f_m[n-1]|$

- Combine the time-frequency variation into ENF estimation

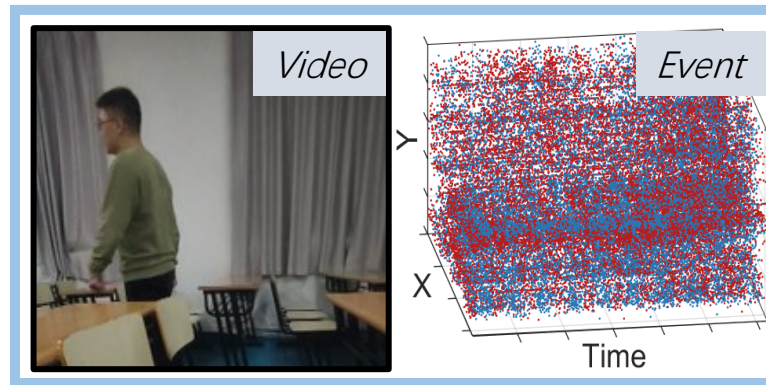
Event-Video hybrid ENF Dataset :

➤ EV-ENFD

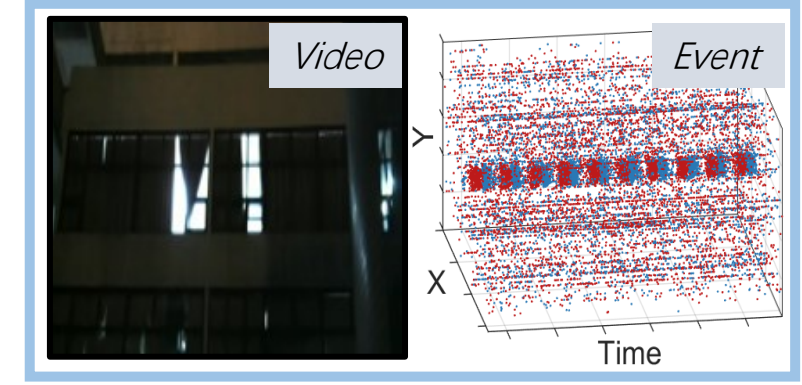
—51 sets of data, each set of data contains two video sequences and one event sequence.



Static Scenes
(16 sets)



Dynamic Scenes
(25 sets)

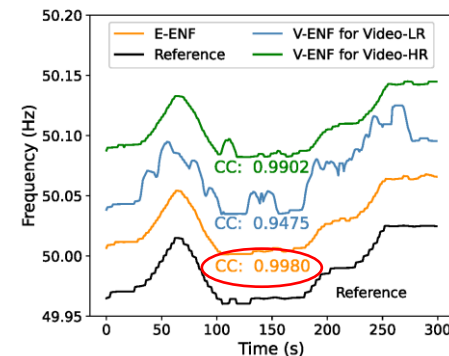
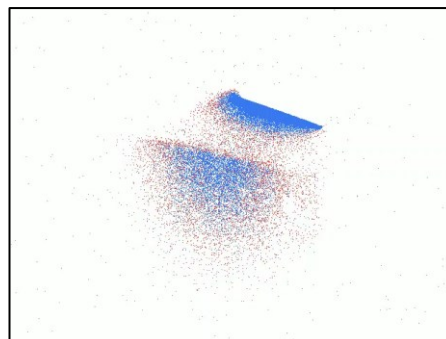


Extreme Lighting
(10 sets)

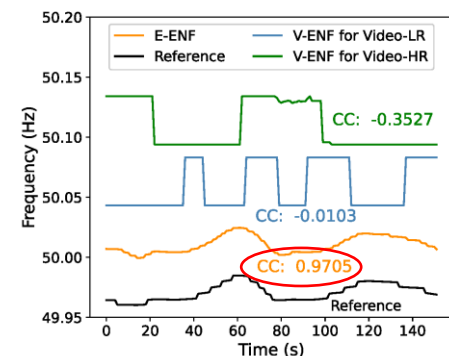
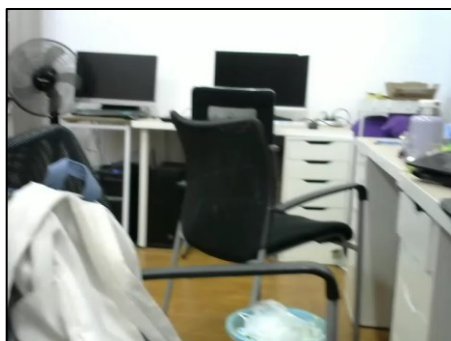
- ❑ A hybrid dataset containing both events and videos recorded in real-world lighting environments.

Results

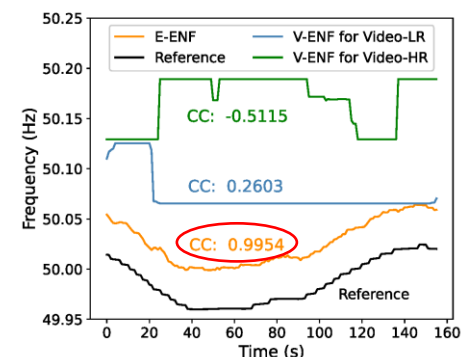
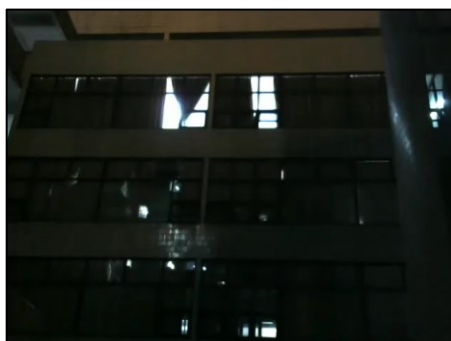
Static Scene



Dynamic Scene



Extreme Lighting



Video

Event

Estimation

- **V-ENF** struggles with dynamic and extreme lighting scenes.

- **E-ENF** exhibits **optimal performance** across three distinct typical scenes.



THANKS

Project Page: <https://xlx-creator.github.io/E-ENF/>

