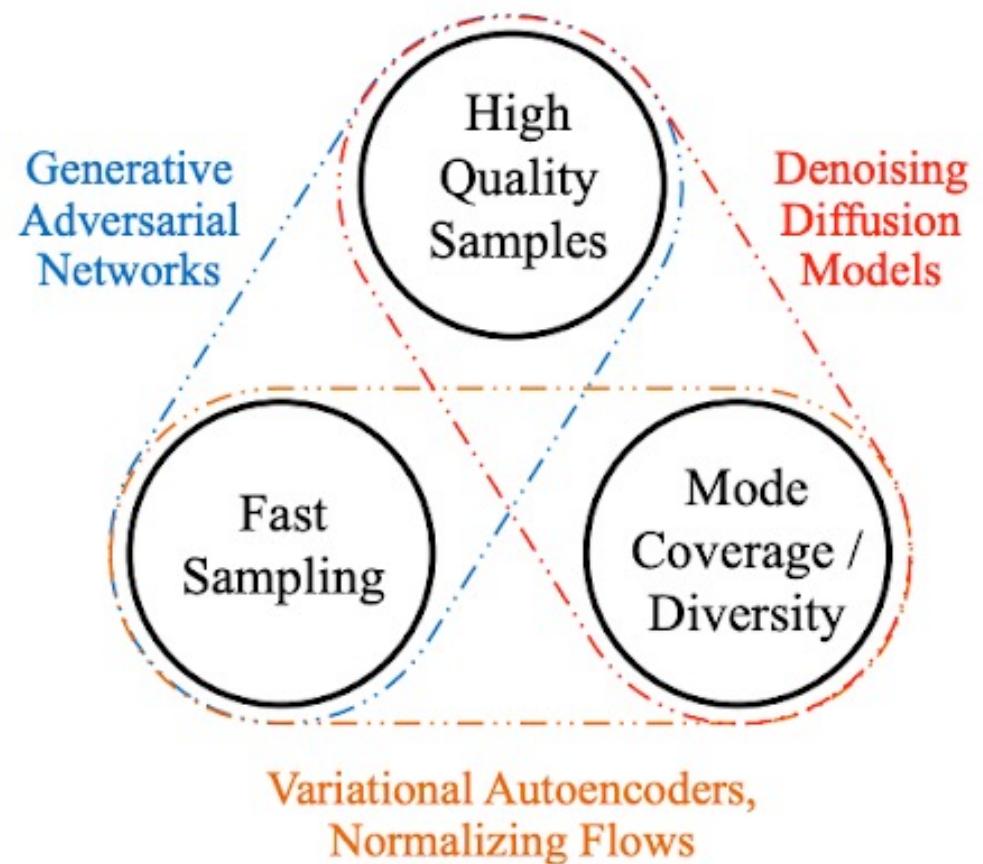


# Diffusion Probabilistic Model Made Slim [CVPR 2023]

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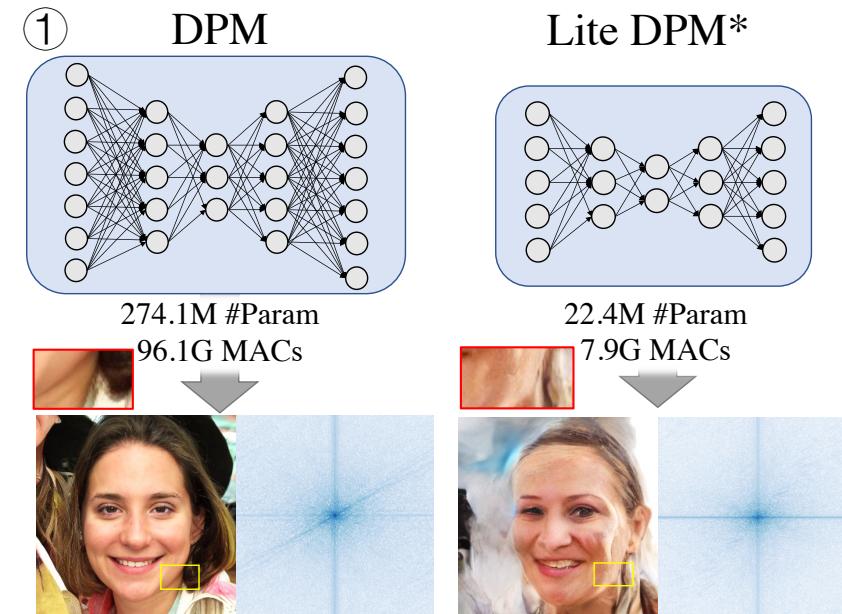
# Challenge: DPM Lacks Efficiency



Method	#Param	FID↓	Low-freq Error↓	High-freq Error↓
LDM	274.1M	5.0	0.11	0.75
Lite-LDM	22.4M	17.3	0.28(+0.17)	3.35(+2.17)

Table 1. Low-freq and High-freq error for different model size.

# Challenge 2: Small Diffusion High-frequency Deficiency



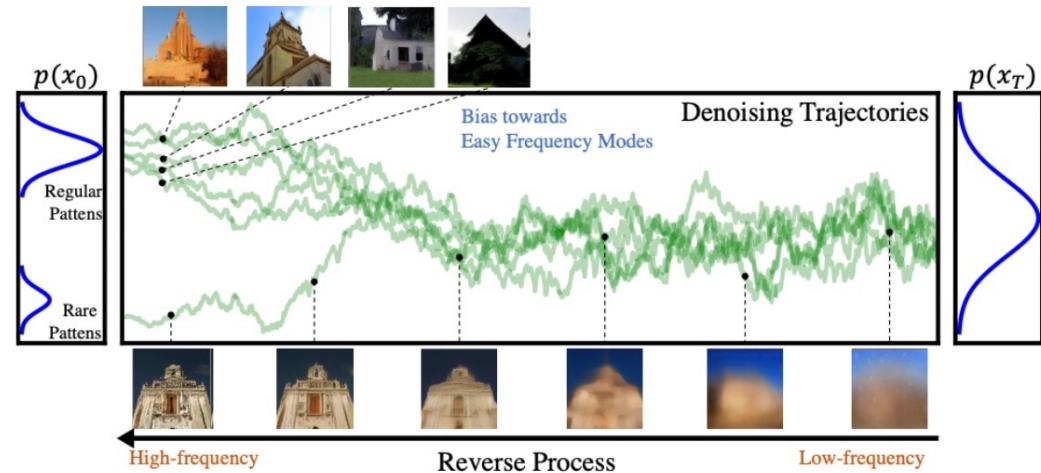
# Frequency Analysis

## 1. Spectrum Evolution

- Low to high recovery

## 2. Frequency Bias

- Deficiency on Long-tail patterns



**Figure 2. Illustration of the Frequency Evolution and Bias for Diffusion Models.** In the reverse process, the optimal filters recover low-frequency components first and add on the details at the end. The predicted score functions may be incorrect for rare patterns, thus failing to recover complex and fine-grained textures.

# I. Spectrum Evolution

Simplified Assumption: Linear Filter, additive Gaussian, wide-sense stationary signal

**Weiner Filter**

**Proposition 1.** Assume  $\mathbf{x}_0$  is a wide-sense stationary signal and  $\epsilon$  is white noise of variance  $\sigma^2 = 1$ . For  $\mathbf{x}_t = \sqrt{\bar{\alpha}}\mathbf{x}_0 + \sqrt{1 - \bar{\alpha}}\epsilon$ , the optimal linear denoising filter  $h_t$  at time  $t$  that minimize  $J_t = \|h_t * \mathbf{x}_t - \epsilon\|^2$  has a closed-form solution

$$\mathcal{H}_t^*(f) = \frac{1}{\bar{\alpha}|\mathcal{X}_0(f)|^2 + 1 - \bar{\alpha}} \quad (6)$$

where  $|\mathcal{X}_0(f)|^2$  is the power spectrum of  $\mathbf{x}_0$  and  $\mathcal{H}_t^*(f)$  is the frequency response of  $h_t^*$ .

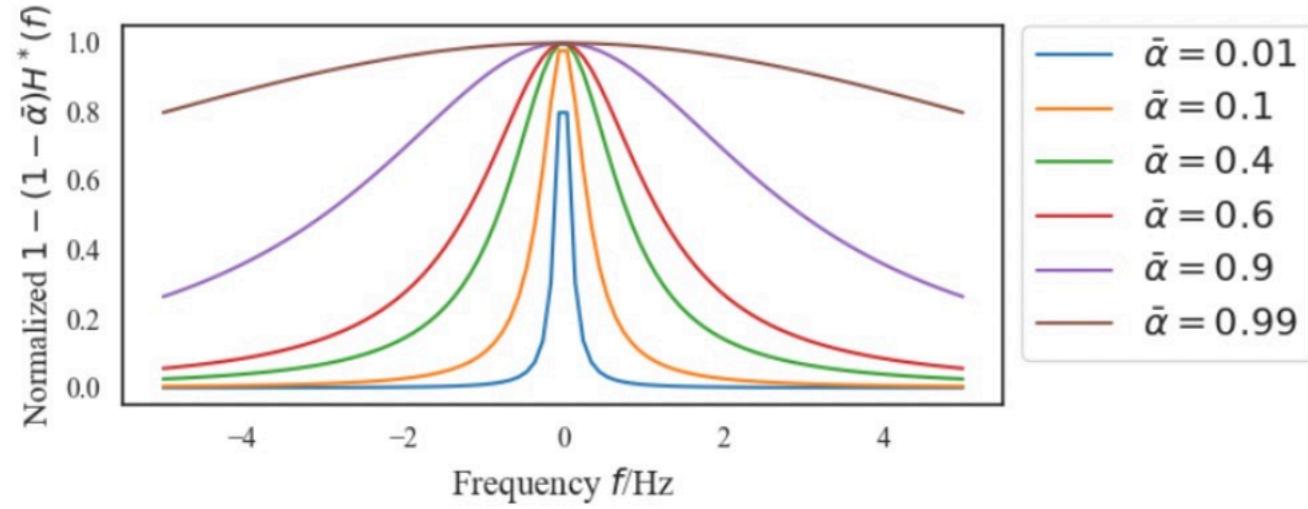
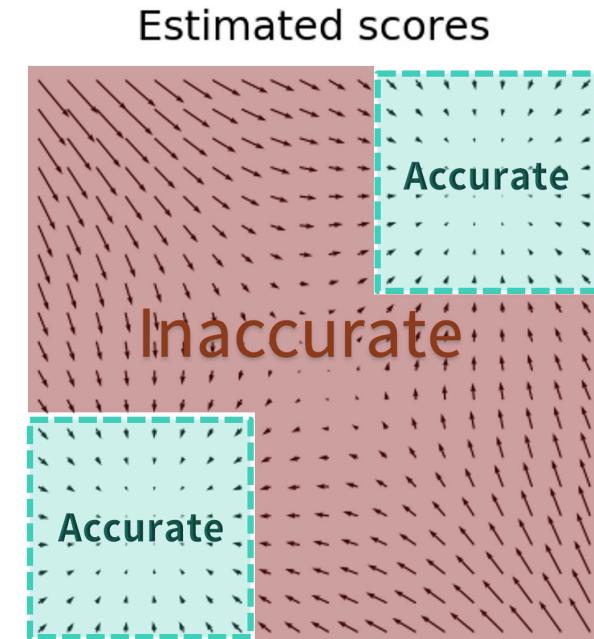
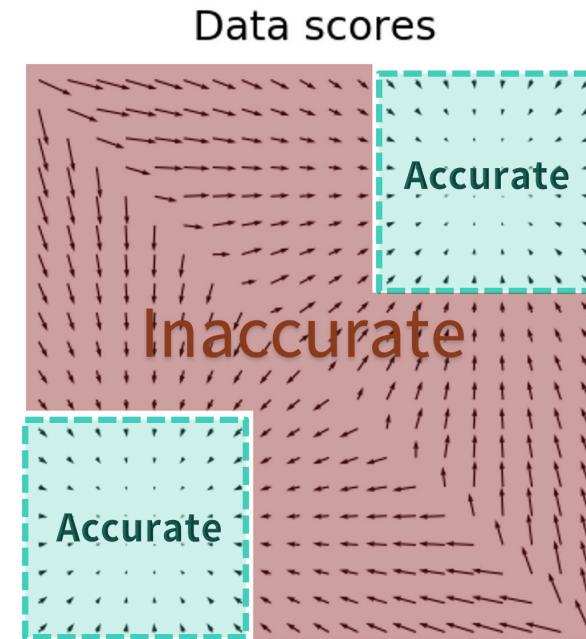
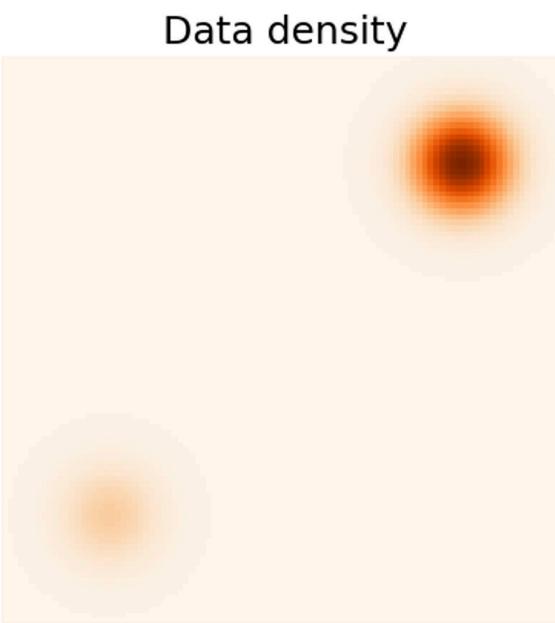


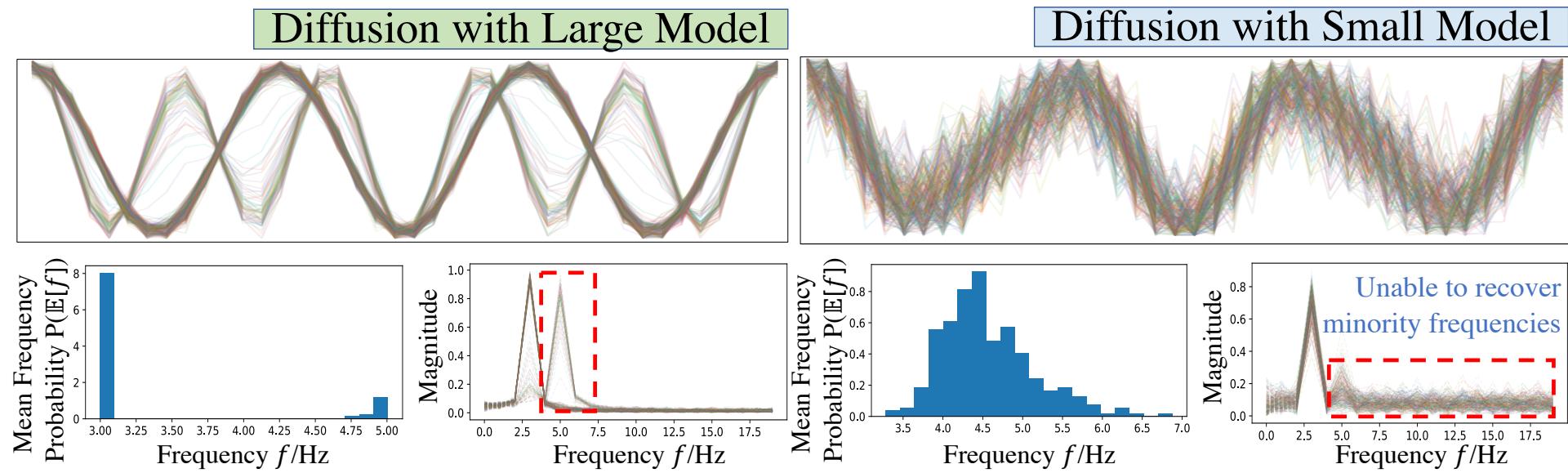
Figure 3.  $1 - (1 - \bar{\alpha})|H^*(f)|^2$  of the optimal linear denoising filter with different  $\bar{\alpha}$ .

# I. Spectrum Evolution

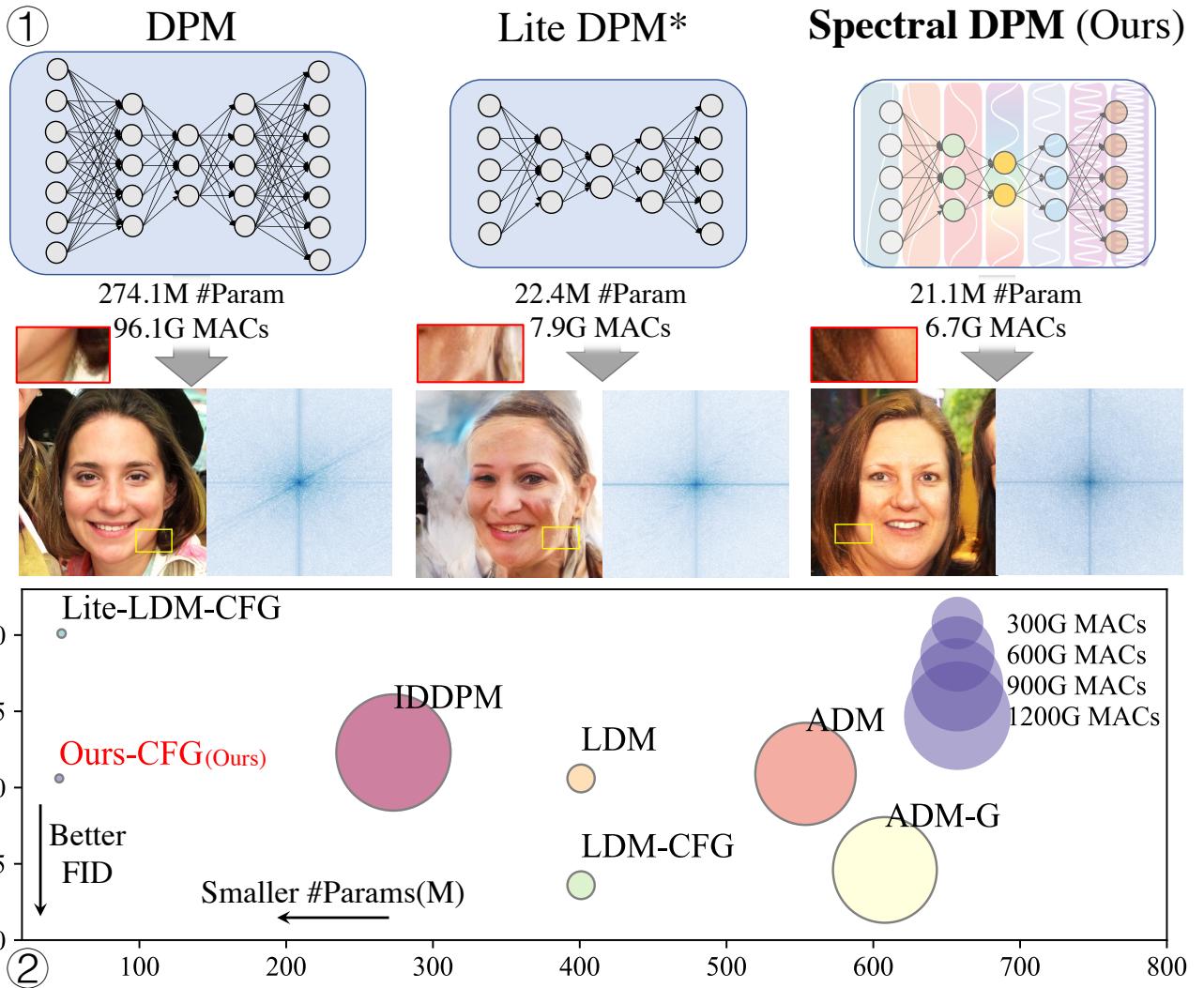
## II. Frequency Deficiency



## II. Frequency Deficiency



# Our solution: Spectral Diffusion



# Module 1 Wavelet Gating

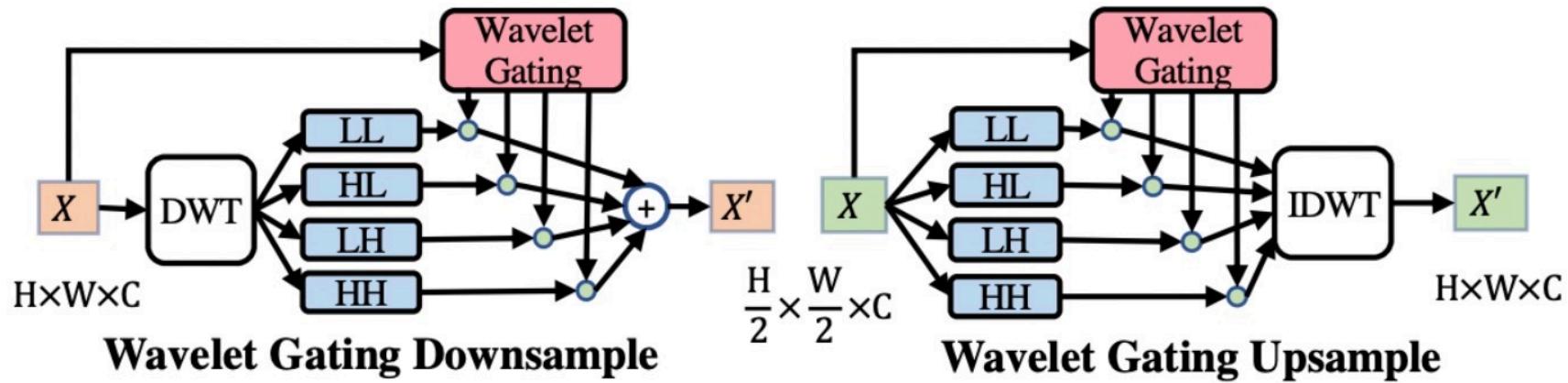
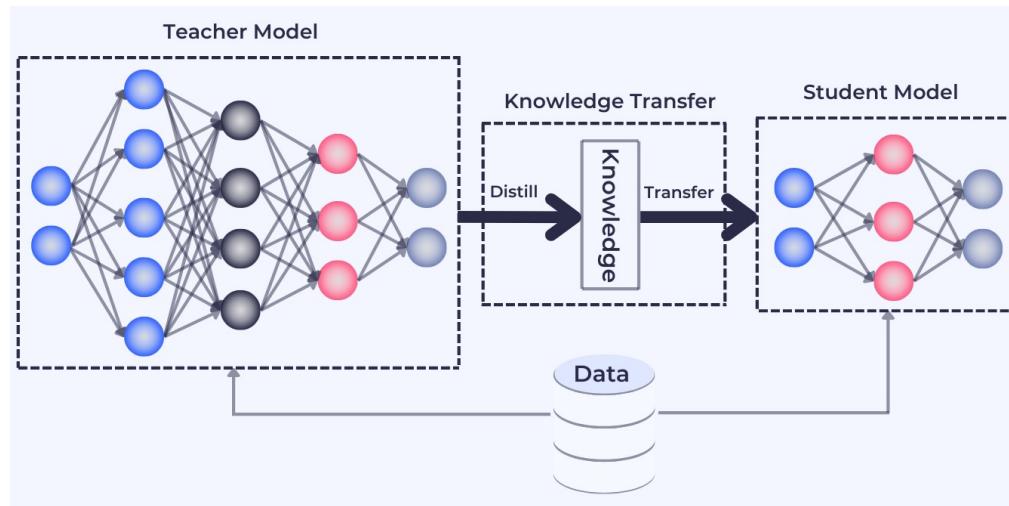


Figure 5. WG-Down and WG-Up with wavelet gating.

Make Diffusion Dynamic, to tackle Challenge 1

# Module 2 Distill High-Frequency



$$\mathcal{X}_T^{(i)} = \mathcal{F}[\mathbf{X}_T^{(i)}], \mathcal{X}_S^{(i)} = \mathcal{F}[\mathbf{X}_S^{(i)}], \mathcal{X}^{(i)} = \mathcal{F}[\text{Resize}(\mathbf{x}_0)]$$

$$\mathcal{L}_{\text{freq}} = \sum_i \omega_i \|\mathcal{X}_T^{(i)} - \mathcal{X}_S^{(j)}\|_2^2, \text{ where } \omega = |\mathcal{X}^{(i)}|^\alpha$$

Boost High-Freq, to tackle Challenge 2

# Quantitative Results

**FFHQ** 256 × 256

Model	#Param	MACs	FID↓
DDPM [18]	113.7M	248.7G	8.4
P2 [6]	113.7M	248.7G	7.0
LDM [48]	274.1M	96.1G	5.0
Lite-LDM	22.4M( <small>12.2×</small> )	7.9G( <small>12.2×</small> )	17.3( <small>-12.3</small> )
Ours	21.1M( <small>13.0×</small> )	6.7G( <small>14.3×</small> )	10.5( <small>-5.5</small> )

**LSUN-Bedroom** 256 × 256

Model	#Param	MACs	FID↓
DDPM [18]	113.7M	248.7G	4.9
IDDPM [42]	113.7M	248.6G	4.2
ADM [8]	552.8M	1114.2G	1.9
LDM [48]	274.1M	96.1G	3.0
Lite-LDM	22.4M( <small>12.2×</small> )	7.9G( <small>12.2×</small> )	10.9( <small>-7.9</small> )
Ours	21.1M( <small>13.0×</small> )	6.7G( <small>14.3×</small> )	5.2( <small>-2.2</small> )

**CelebA-HQ** 256 × 256

Model	#Param	MACs	FID↓
Score SDE [59]	65.57M	266.4G	7.2
DDGAN [62]	39.73M	69.9G	7.6
LDM [48]	274.1M	96.1G	5.1
Lite-LDM	22.4M( <small>12.2×</small> )	7.9G( <small>12.2×</small> )	14.3( <small>-9.2</small> )
Ours	21.1M( <small>13.0×</small> )	6.7G( <small>14.3×</small> )	9.3( <small>-4.2</small> )

**LSUN-Church** 256 × 256

Model	#Param	MACs	FID↓
DDPM [18]	113.7M	248.7G	4.9
IDDPM [42]	113.7M	248.6G	4.3
ADM [8]	552.8M	1114.2G	1.9
LDM [48]	295.0M	18.7G	4.0
Lite-LDM	32.8M( <small>9.0×</small> )	2.1G( <small>8.9×</small> )	13.6( <small>-9.6</small> )
Ours	33.8M( <small>8.7×</small> )	2.1G( <small>8.9×</small> )	8.4( <small>-4.4</small> )

Table 2. Unconditional generation results comparison to prior DPMs. The results are taken from the original paper, except that DDPM is take from the [6].

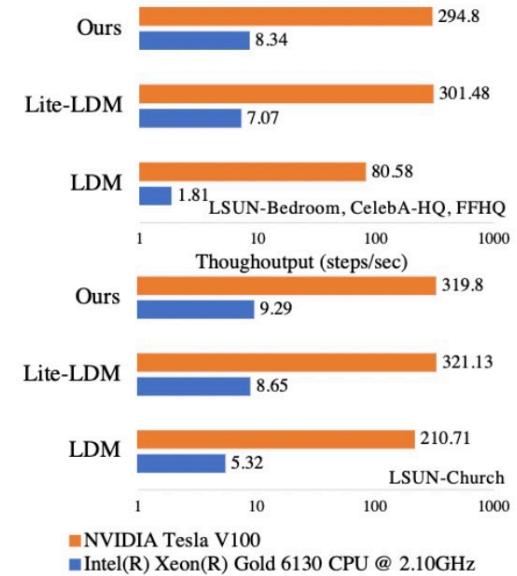


Figure 6. Throughput for unconditional image generation.

# Quantitative Results

Method	#Param	MACs	FID↓
IDDPM [42]	273.1M	1416.3G	12.3
ADM [8]	553.8M	1114.2G	10.9
LDM [48]	400.9M	99.8G	10.6
ADM-G [8]	553.8+54.1M	1114.2+72.2G	4.6
LDM-CFG [48]	400.9M	99.8G	3.6
Lite-LDM-CFG	47.0M( <sup>8.5</sup> ×	11.1G ( <sup>9.0</sup> ×	20.1( <sup>-16.5</sup> )
Ours-CFG	45.4M( <sup>8.8</sup> ×	9.9G ( <sup>10.1</sup> ×	10.6( <sup>-7.0</sup> )

Table 3. Comparison of class-conditional image generation methods on ImageNet [7] with recent state-of-the-art methods. “G” stands for the classifier guidance and “CFG” refers to the classifier-free guidance for conditional image generation.

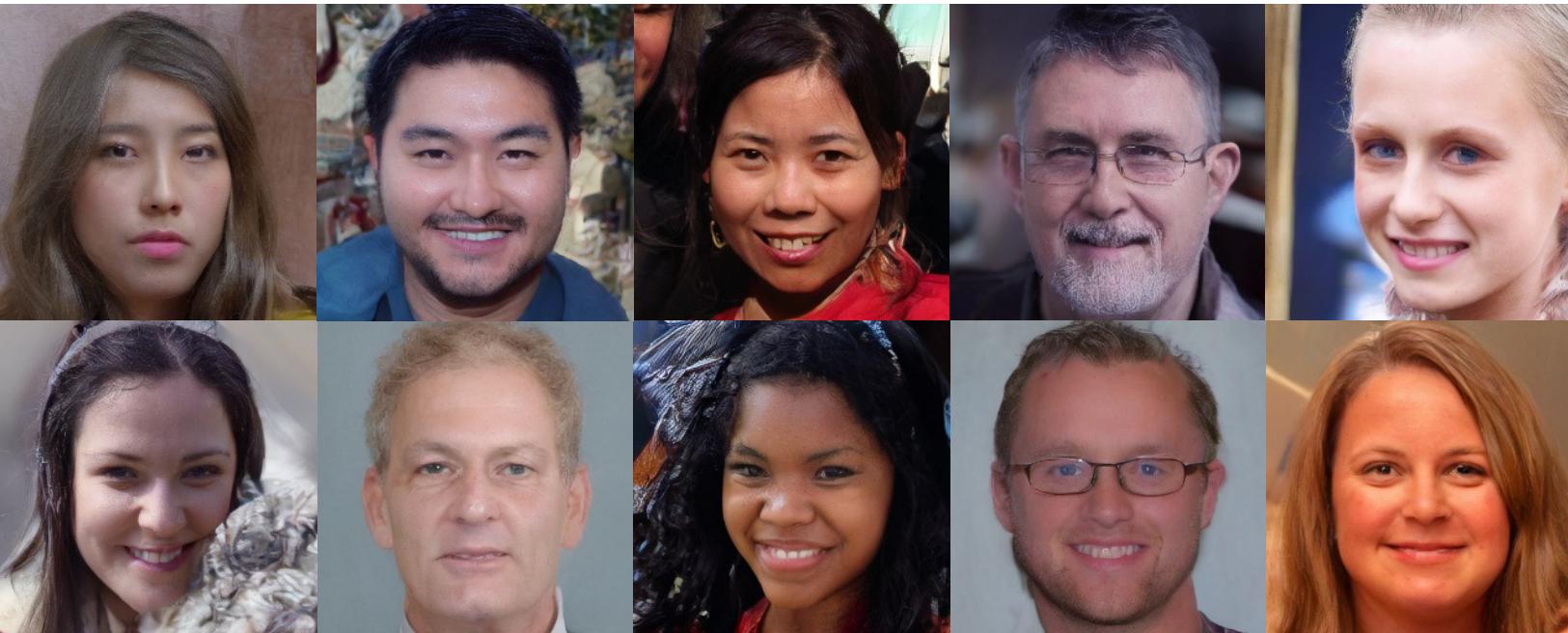
Method	#Param	FID↓
GLIDE [41]	5.0B	12.24
DALLE2 [45]	5.5B	10.39
Imagen [51]	3.0B	7.27
LDM [48]	1.45B	12.63
Ours	77.6M( <sup>18.7</sup> ×	18.87

Table 4. Zero-Shot FID on MS-COCO text-to-image generation.

# Visualizations: CelebA-HQ



# Visualizations: FFHQ



# Visualizations: ImageNet



# Ablation Study

Method	<b>FFHQ 256 × 256</b>							
+ Wavelet Gating	✓			✓		✓		✓
+ Spatial Distill		✓		✓	✓	✓		✓
+ Freq Distill			✓		✓	✓	✓	✓
FID↓	17.3	14.7	16.6	15.3	12.3	12.4	11.4	10.5

Table 5. Ablation study on FFHQ dataset.

# Ablation Study

- + Lite-LDM lacks recovery for high-freq
- + Our SD gets better high-freq reconstruction

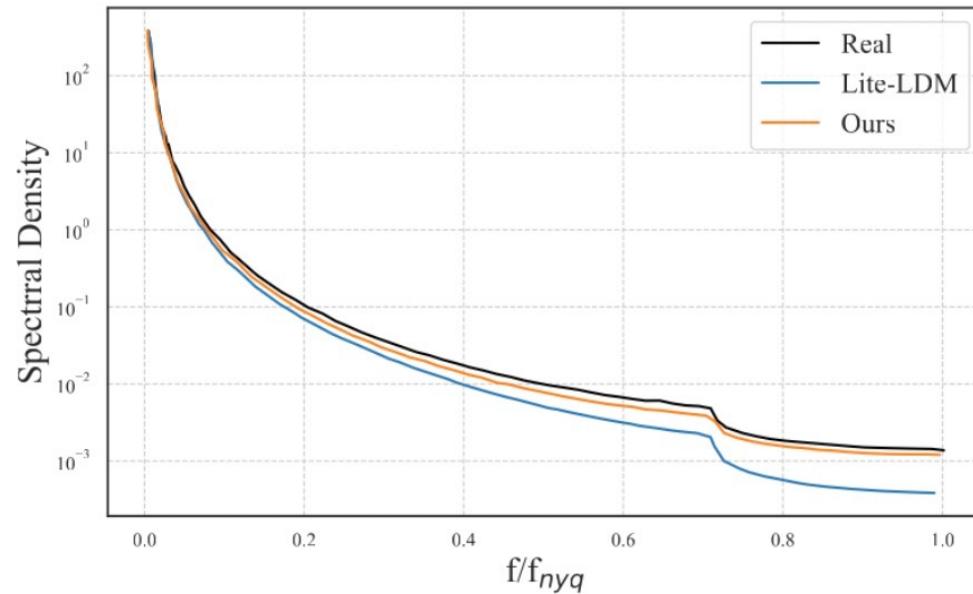


Figure 3. Mean reduced spectrum from real and generated images.

**Thanks for Listening**