

ISTITUTO ITALIANO DI TECNOLOGIA PATTERN ANALYSIS AND COMPUTER VISION



DiffAssemble: A Unified Graph-Diffusion Model for 2D and 3D Reassembly

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2D & 3D Reassembly Tasks

Problem. Placing each individual component in its correct position and orientation to form a coherent structure







DiffAssemble

General framework for solving reassembly tasks using graph representations and a diffusion model formulation



Graph Formulation

Features h $\in \mathbb{R}^d \rightarrow$ Features generated by a backbone **Position s** $\in \mathbb{R}^n \rightarrow$ Represent the dimensionality of the continuous Euclidean space **Rotation** $R \in SO(n) \rightarrow$ Represent the matrix belonging to the Special Orthogonal Group in *n* dimensions. We also define **r**, where $f_r(\mathbf{r}) = R$.





The Key Point of Using Diffusion

Create random starting scenarios and learn how to reverse this process step by steps



Reverse Denoising Process (Inference)

Forward Diffusion Process (Training)



3D Reassembly Task: Breaking Bad

Number of Objects. Contains around 10k meshes from PartNet and Thingi10k.

Pieces. Number of re-compute 20 fracture modes and then simulate 80 fractures from them, resulting in a total of 1,047,400 breakdown patterns.

Subsets. Everyday, Artifact and Other to facilitate different applications.



[1] Sellán, Silvia, et al. "Breaking bad: A dataset for geometric fracture and reassembly." Advances in Neural Information Processing Systems 35 (2022).



3D Reassembly Task: Results

Method	$\frac{\text{RMSE}(R)\downarrow}{\text{degree}}$	$\frac{\text{RMSE}(T)\downarrow}{\times 10^{-2}}$	PA↑ %	
Global [34]	81.6	15.2	17.5	-
DGL [34]	81.4	<u>14.9</u>	25.4	
LSTM [34]	87.4	15.8	11.3	· ·
SE(3)-Equiv [46]	<u>77.9</u>	16.7	8.1	
DiffAssemble - No Diffusion Process	83.6	17.1	3.1	
DiffAssemble - No Equivariant Enc.	81.7	17.0	18.3	
DiffAssemble	73.3	14.8	27.5	

Insights

- No trade accuracy between rotation and translation
- Benefit in deploying the Diffusion Process and the Equivariant Backbone



2D Reassembly Task: Dataset





CelebA-HQ. Contains 30K images of celebrities in High Definition (HD). The images are cropped and positioned to show only centered faces.[1]

WikiArt. Contains 63K images of paintings in HD. This dataset contains paintings with very different content and artistic styles.[2]

[1] Lee, Cheng-Han, et al. "Maskgan: Towards diverse and interactive facial image manipulation." *Proceedings of the IEEE/CVF conference on computer vision and pattern recognition*. 2020.

[2] Tan, Wei Ren, et al. "Improved ArtGAN for conditional synthesis of natural image and artwork." IEEE Transactions on Image Processing 28.1 (2018).



2D Reassembly Task: Results

		DATASET							
Method		PuzzleCelebA			PuzzleWikiArts				
		6x6	8x8	10x10	12x12	6x6	8x8	10x10	12x12
Optimization Based	Gallagher [15]	80.21	55.18	71.19	69.81	71.88	61.63	54.15	44.68
	Yu <i>et al</i> . [48]	98.63	<u>94.65</u>	98.33	93.33	94.62	92.95	90.99	89.88
	Huroyan <i>et al</i> . [21]	98.47	97.45	98.65	<u>97.08</u>	<u>92.69</u>	<u>91.37</u>	<u>89.74</u>	88.28
Learning Based	DiffAssemble - No Diff.	<u>99.43</u>	79.84	99.05	91.28	73.07	54.70	22.68	18.27
	DiffAssemble - No Equiv.	96.12	71.62	91.98	64.15	25.31	14.63	8.19	4.96
	DiffAssemble	99.51	87.66	99.30	97.76	90.65	72.79	63.33	53.08

	DATASET					
Method	CelebA	WikiArts				
	6x6 12x12	6x6 12x12				
Gallagher [15]	33.28 19.18 (-46.93) (-50.63)	32.19 24.12 (-39.69) (-20.56)				
Yu [21]	$\frac{33.45}{(-66.85)} \frac{21.78}{(-72.84)}$	$\frac{32.53}{(-62.09)} \frac{24.65}{(-65.23)}$				
Huroyan [48]	18.18 0.09 (-80.29) (-88.45)	17.14 0.08 (-75.55) (-80.28)				
DiffAssemble	96.92 76.49 (-2.59) (-32.81)	51.21 27.09 (-39.44) (-25.99)				

Insights

- We do not rely only on visual appearances but also on the semantic content
- We are robust to real-scenarios like missing pieces



Scaling to Larger Graphs: Results

Dataset. PuzzleCelebA **Implementation Details.** Puzzles of 900 pieces (30 x 30 puzzles)





Insights

• The sparsity attention mechanism reduces 2.5x the GPU memory

Insights

- Faster than optimization-based model
- No reduction in Accuracy



Conclusion & Future Work

- Introduction of DiffAssemble, a general framework for tackling sorting tasks via graph representations and a diffusion model formulation
- Demonstration of the effectiveness of our method spanning 3D object reassembly and 2D puzzles with translated and rotated pieces:
 - Robustness compared to optimization-based methods
 - State-of-the-art results in 3D domain
 - Possibility to scale on larger graphs

