

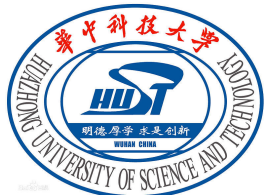


# Towards Efficient Replay in Federated Incremental Learning

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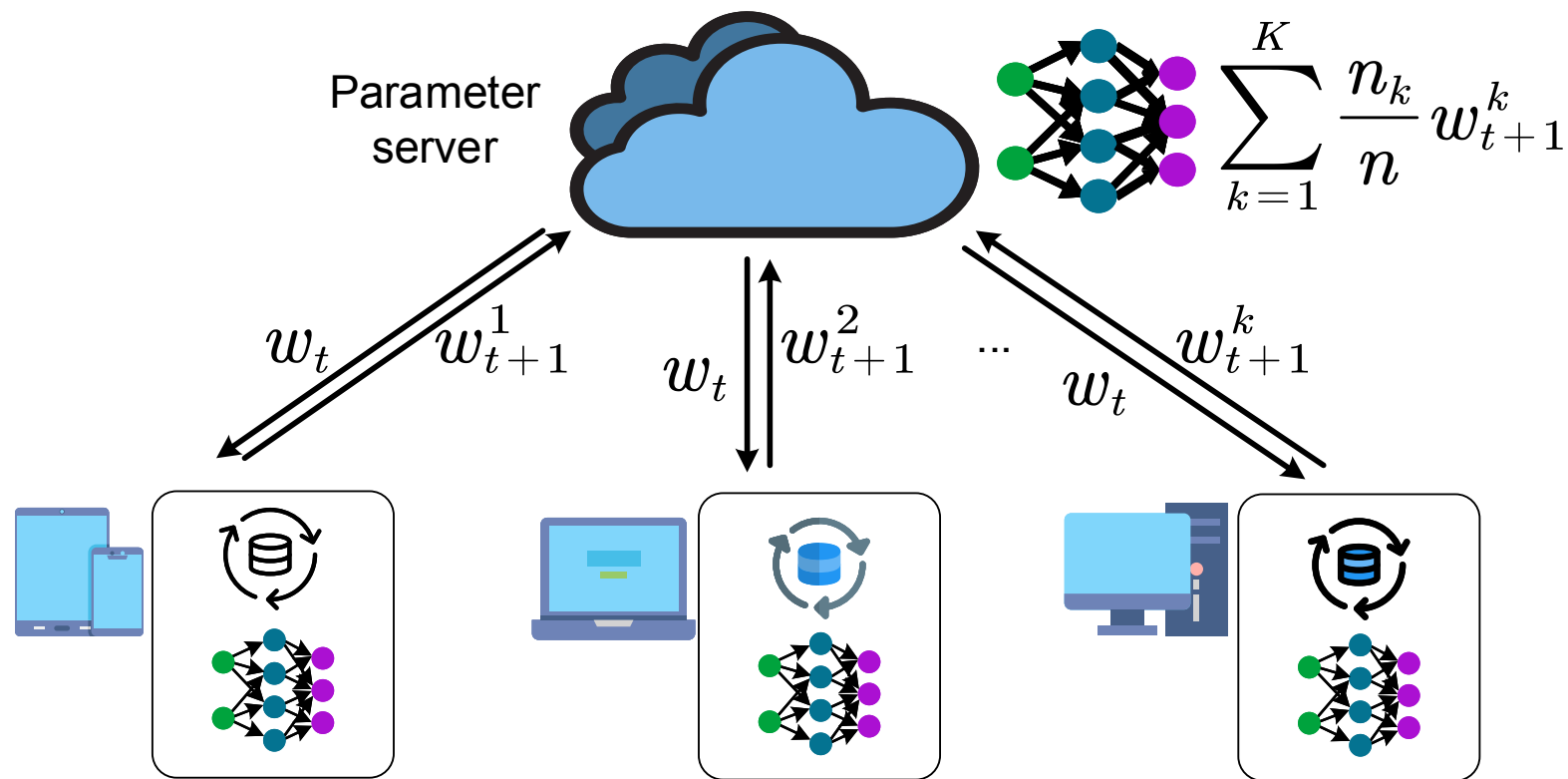


# Federated Incremental Learning

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- I. Background**
- II. Limitations and Motivations**
- III. Methodology and Theory**
- IV. Experimental Results**
- V. Conclusion**

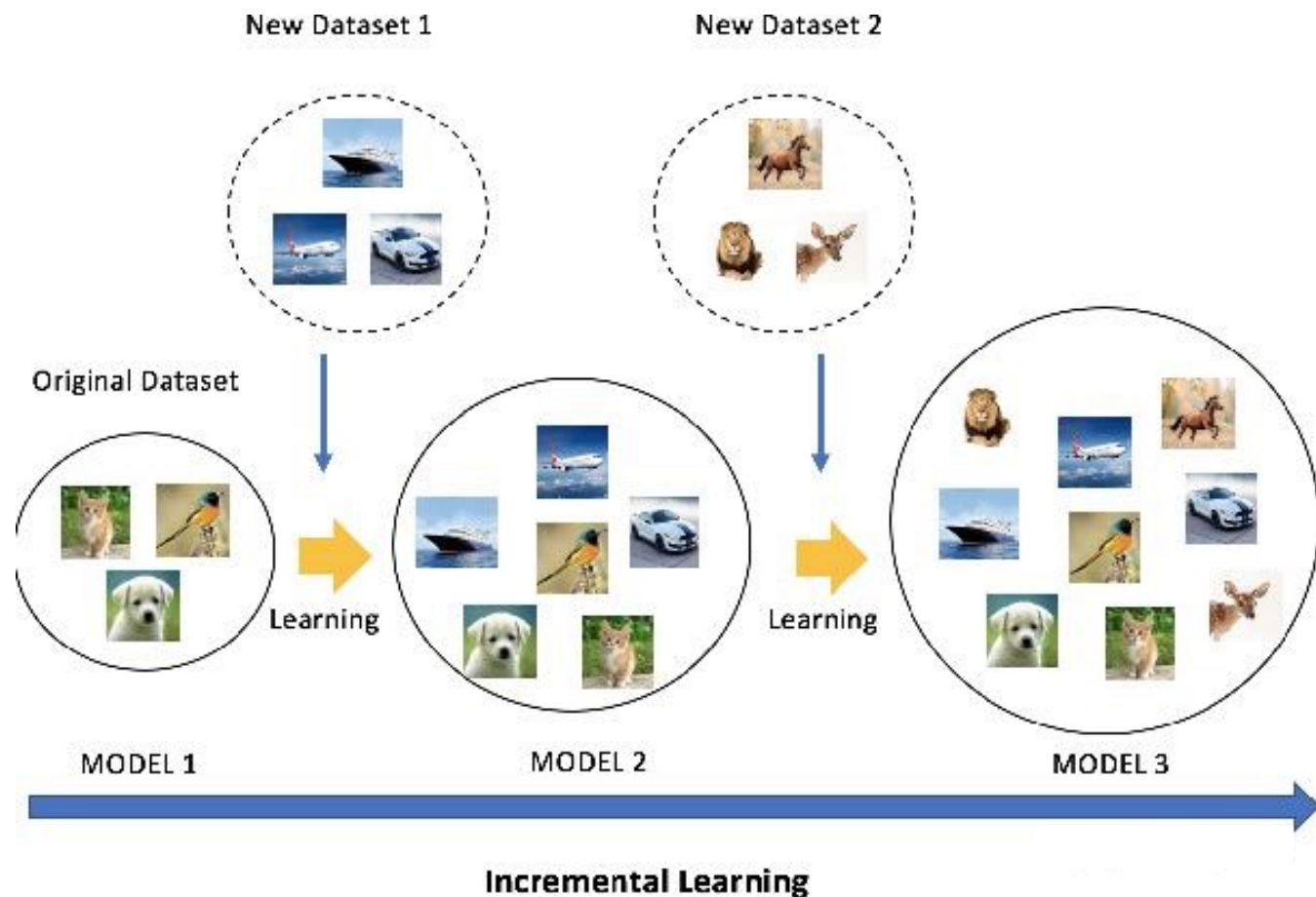
# Background: Federated Learning



**FedAvg: Global model is obtained by computing the average of parameters of multiple local models**

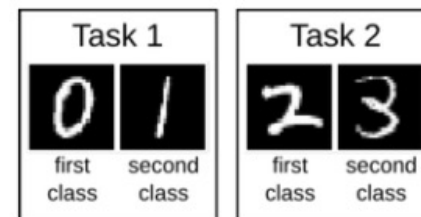
# Background: Continual Learning

Illustration of Continual Learning/Incremental Learning/Lifelong Learning



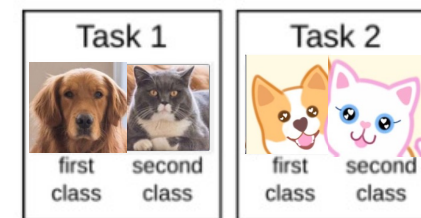
Three Typical Scenarios

- **Class-Incremental Learning**



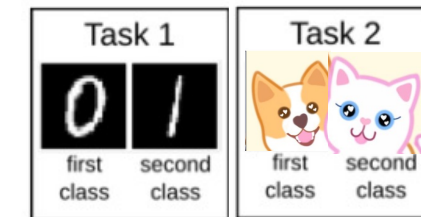
$$P(Y^1) \neq P(Y^2)$$

- **Domain-Incremental Learning**



$$P(X^1) \neq P(X^2)$$

- **Task-Incremental Learning**

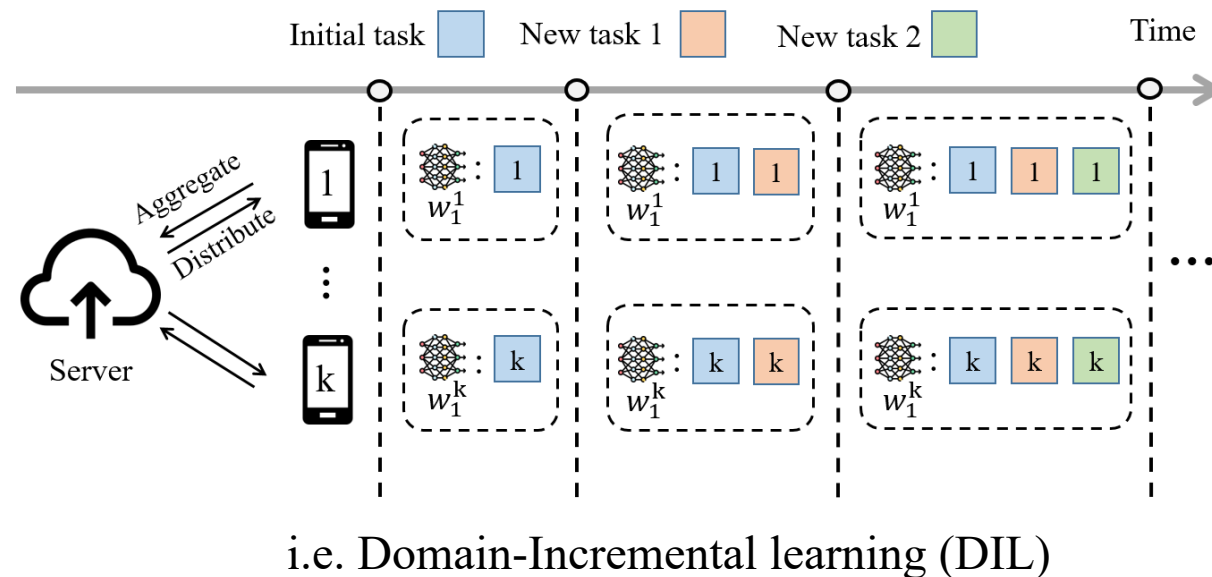


$$P(Y^1) \neq P(Y^2), P(X^1) \neq P(X^2), |Y^1| \neq |Y^2|$$

# Limitations

- ◆ **Dynamic:** existing FL methods typically assume the data in each client is fixed or static.
  - data often comes in an incremental manner, where the data domain may increase dynamically.
- ◆ **Catastrophic Forgetting:** clients are difficult to learn new data while retaining previous information
  - especially when data is non-identically and independently distributed (Non-IID) across clients.

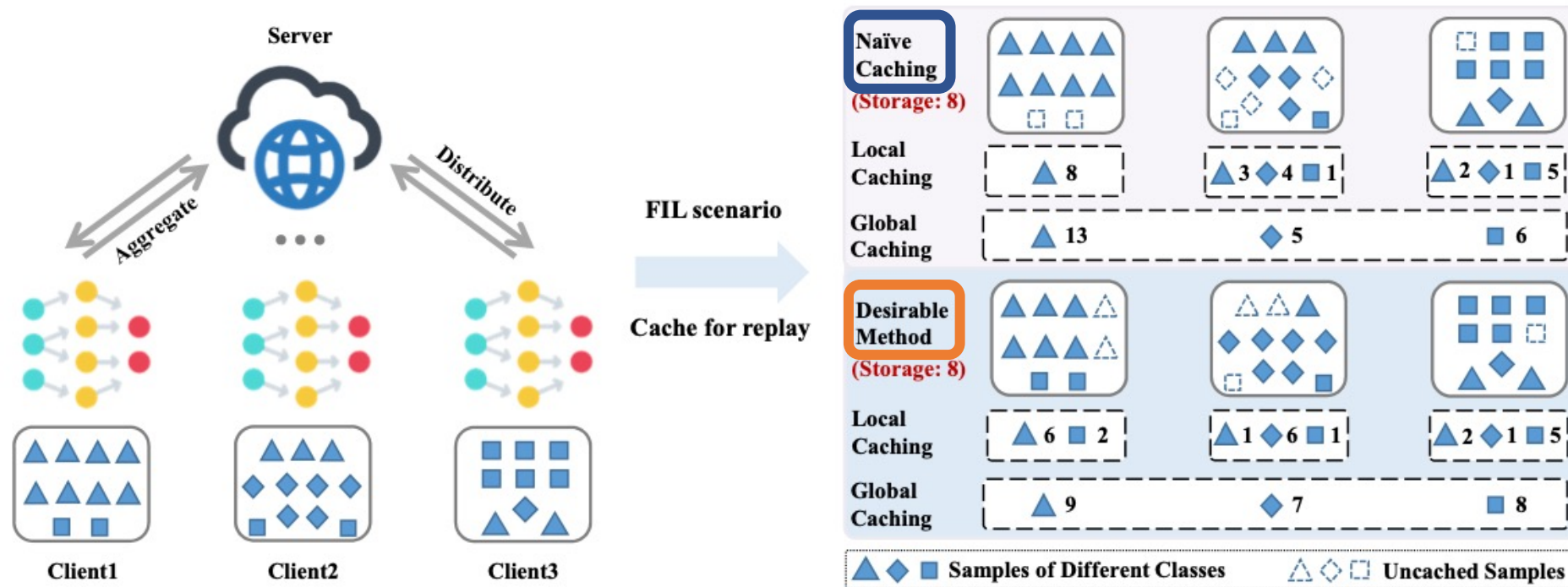
		Spatial heterogeneity			
		No changes (IID data)	Changes in the input space throughout clients $P_i(x) \neq P_j(x)$	Changes in the behaviour throughout clients $P_i(y x) \neq P_j(y x)$	Changes in the input space and behaviour throughout clients
Temporal heterogeneity	No changes (IID data)	OUT OF SCOPE	[35–38, 44] [55, 61–81]	[39–42] [99–101]	[45] [50–52]
	Changes in the input space over time, $P^l(x) \neq P^{l+k}(x)$ (Virtual Concept Drift)	[8, 117–122] [131–137]	NOT ADDRESSED SO FAR		
	Changes in the behaviour over time, $P^l(y x) \neq P^{l+k}(y x)$ (Real Concept Drift)	[123–125] [138–144]			
	Changes in the input space and behaviour over time (Total Concept Drift)	NO SPECIFIC ALGORITHMS			



# Motivations

- ◆ **Assumption:** each client can cache a few samples with the local storage for replay
- lack enough storage space to retain full data

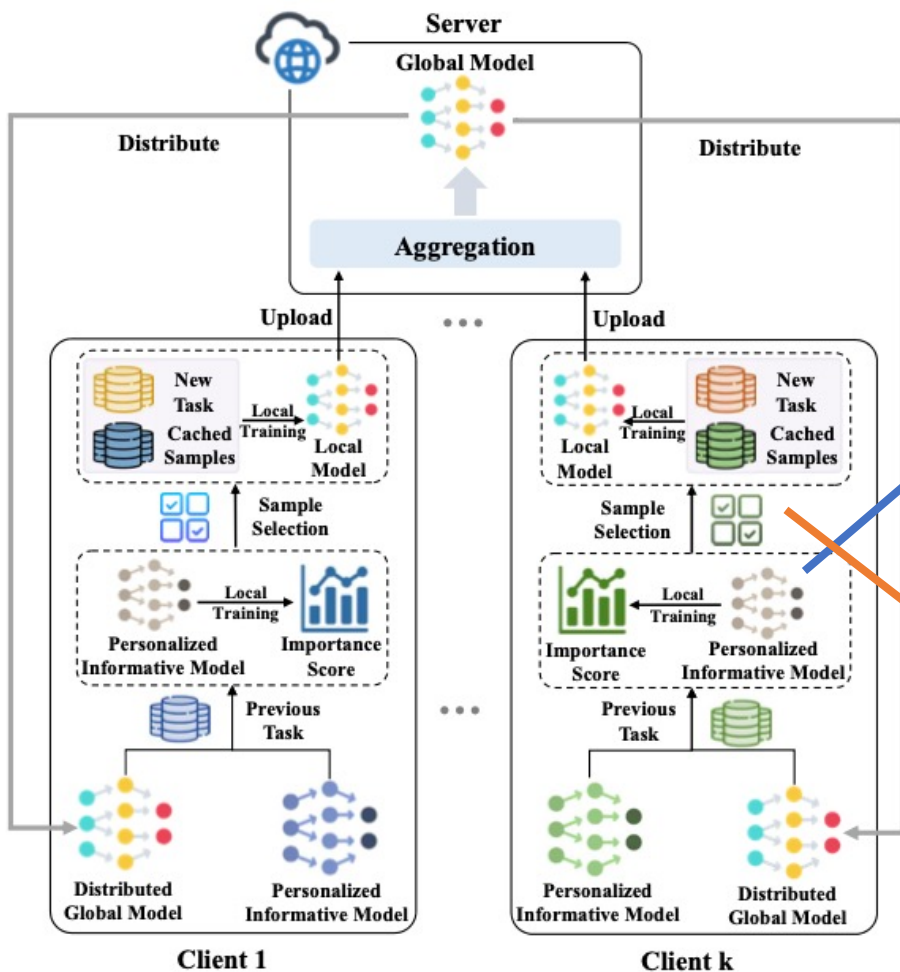
## An example of 3-client in FIL scenario



**Synergistic Replay with Important Samples !**

# Methodology: Re-Fed

- How to ensure that samples can balance local training and global data distribution?
- How to quantify the importance of samples?



## ◆ Personalized Informative Model

$$v_{k,s}^{t-1} = v_{k,s-1}^{t-1} - \eta \left( \sum_{i=1}^M \nabla l \left( f_{v_{k,s-1}^{t-1}}(\tilde{x}_{k,t-1}^{(i)}), \tilde{y}_{k,t-1}^{(i)} \right) + q(\lambda)(v_{k,s-1}^{t-1} - w^{t-1}) \right). \quad (3)$$

## ◆ Sample Importance Score

$$G^p(\tilde{x}_{k,t-1}^{(i)}) = \left\| \nabla l \left( f_{v_{k,p}^{t-1}}(\tilde{x}_{k,t-1}^{(i)}), \tilde{y}_{k,t-1}^{(i)} \right) \right\|^2. \quad (4)$$

$$I(\tilde{x}_{k,t-1}^{(i)}) = \sum_{p=1}^s \frac{1}{p} G^p(\tilde{x}_{k,t-1}^{(i)}). \quad (5)$$

**Lemma 1** (Proportion of Global and Local Information.) *For all  $\lambda \in (0, 1)$  and  $\lambda \rightarrow f(\lambda_k)$  is non-increasing:*

$$\begin{aligned} \frac{\partial \nabla f(\hat{v}_k(\lambda))}{\partial \lambda} &\leq 0 \\ \frac{\partial \|\hat{v}_k(\lambda) - \hat{w}\|}{\partial \lambda} &\geq 0. \end{aligned} \tag{11}$$

Then, for  $k \in [K]$ , we can get:

$$\lim_{\lambda \rightarrow 0} \hat{v}_k(\lambda) := \hat{w}. \tag{12}$$

**Lemma 2** ([21] Lemma 13.) Under assumptions above,  $f(v_k)$  is  $\mu_k$ -strongly convex at each communication round  $t$ , we have:

$$\begin{aligned} \mathbb{E} \left[ \|v_k^{t+1} - \hat{v}_k\|^2 \right] &\leq (1 - \eta(\mu_k + q(\lambda))) \mathbb{E} \left[ \|v_k^t - \hat{v}_k\|^2 \right] + \eta^2 \left( \sigma + q(\lambda) \left( M + \frac{\sigma}{\mu_k} \right) \right)^2 + \eta^2 q(\lambda)^2 \mathbb{E} \left[ \|w^t - \hat{w}\|^2 \right] \\ &\quad + 2\eta^2 q(\lambda) \left( \sigma + q(\lambda) \left( M + \frac{\sigma}{\mu_k} \right) \right) \sqrt{\mathbb{E} \left[ \|w^t - \hat{w}\|^2 \right]} + 2\eta q(\lambda) \sqrt{\mathbb{E} \left[ \|v_k^t - \hat{v}_k\|^2 \right] \mathbb{E} \left[ \|w^t - \hat{w}\|^2 \right]}. \end{aligned} \tag{13}$$

**Theorem 3.1** (Personalized Informative Model.) *Assuming the global model  $w^t$  converges to the optimal model  $\hat{w}$  with  $g(t)$  for any client  $k \in [K]$  at each communication round  $t$ :  $\mathbb{E} \left[ \|w^t - \hat{w}\|^2 \right] \leq g(t)$  and  $\lim_{t \rightarrow \infty} g(t) = 0$ , then there exists a constant  $C < \infty$  such that the personalized informative model  $v_k^t$  can converge to the optimal model  $\hat{v}_k$  with  $Cg(t)$ .*



## Datasets

### Class-Incremental Learning

- ◆ CIFAR10
- ◆ CIFAR100
- ◆ Tiny-ImageNet

### Domain-Incremental Learning

- ◆ Digit10
- ◆ Office31
- ◆ Domain Net

## Baselines

### Traditional FL Methods

- ◆ FedAvg
- ◆ FedProx

### Customed Methods

- ◆ Fixed
- ◆ DANN+FL
- ◆ Shared

### Existing FIL Methods

- ◆ FCIL
- ◆ FedDIL

# Experiments - Performance Overview

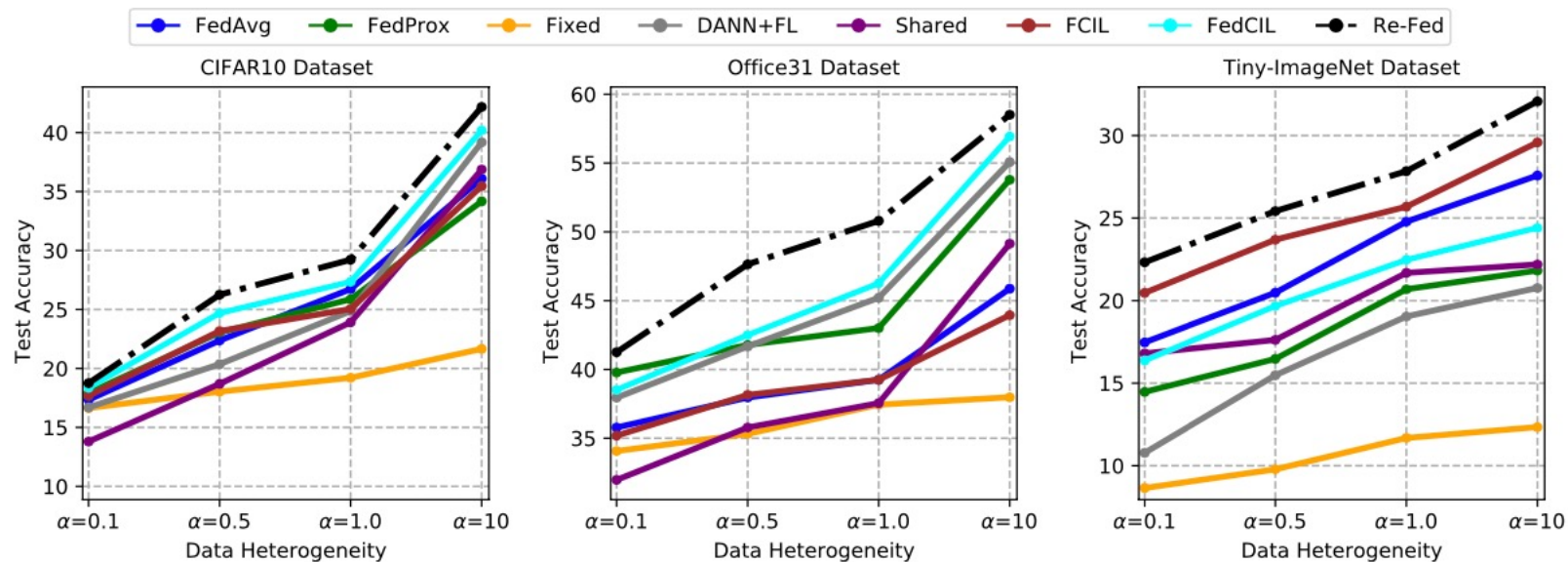
## Test Accuracy & Communication Efficiency

Scenario	Dataset	FedAvg	FedProx	Fixed	DANN+FL	Shared	FCIL	FedCIL	Re-Fed
Class-Incremental	CIFAR10 ( $\alpha = 1.0$ )	26.73 $\pm$ 1.12	25.87 $\pm$ 0.68	19.21 $\pm$ 0.06	24.86 $\pm$ 2.31	23.91 $\pm$ 1.70	25.04 $\pm$ 0.11	27.35 $\pm$ 1.24	<b>29.22<math>\pm</math>0.49</b>
	CIFAR100 ( $\alpha = 5.0$ )	17.21 $\pm$ 1.35	18.03 $\pm$ 0.91	9.27 $\pm$ 0.22	19.73 $\pm$ 2.17	18.30 $\pm$ 1.53	23.02 $\pm$ 0.66	17.98 $\pm$ 1.46	<b>25.61<math>\pm</math>0.88</b>
	Tiny-ImageNet ( $\alpha = 10$ )	27.58 $\pm$ 0.74	21.82 $\pm$ 0.90	12.34 $\pm$ 0.23	20.77 $\pm$ 1.31	22.19 $\pm$ 0.54	29.58 $\pm$ 0.15	24.41 $\pm$ 0.95	<b>32.07<math>\pm</math>0.27</b>
Domain-Incremental	Digit10 ( $\alpha = 0.1$ )	77.59 $\pm$ 0.39	79.09 $\pm$ 0.58	71.26 $\pm$ 0.04	76.44 $\pm$ 1.05	74.77 $\pm$ 0.23	77.59 $\pm$ 0.39	83.85 $\pm$ 0.80	<b>85.96<math>\pm</math>0.14</b>
	Office31 ( $\alpha = 1$ )	39.25 $\pm$ 1.61	43.01 $\pm$ 1.59	37.44 $\pm$ 0.72	45.21 $\pm$ 2.10	37.55 $\pm$ 0.69	39.25 $\pm$ 1.61	46.26 $\pm$ 2.24	<b>50.80<math>\pm</math>0.77</b>
	DomainNet ( $\alpha = 10$ )	51.73 $\pm$ 2.32	49.12 $\pm$ 2.71	46.30 $\pm$ 1.42	50.01 $\pm$ 3.31	41.76 $\pm$ 1.26	51.73 $\pm$ 2.32	47.28 $\pm$ 3.01	<b>56.66<math>\pm</math>0.50</b>

Scenario	Dataset	FedAvg	FedProx	Fixed	DANN+FL	Shared	FCIL	FedCIL	Re-Fed
Class-Incremental	CIFAR10 (Task:5)	613 $\pm$ 2.67	685 $\pm$ 3.00	142 $\pm$ 0.67	712 $\pm$ 3.67	574 $\pm$ 1.33	590 $\pm$ 2.67	738 $\pm$ 4.00	<b>562<math>\pm</math>1.67</b>
	CIFAR100 (Task:10)	1103 $\pm$ 2.33	1246 $\pm$ 3.00	137 $\pm$ 2.00	1258 $\pm$ 4.67	1154 $\pm$ 3.33	1095 $\pm$ 2.67	1311 $\pm$ 5.67	<b>1039<math>\pm</math>4.33</b>
	Tiny-ImageNet (Task:10)	1197 $\pm$ 2.67	1234 $\pm$ 2.67	132 $\pm$ 3.00	1305 $\pm$ 3.67	1278 $\pm$ 4.33	1185 $\pm$ 2.33	1317 $\pm$ 3.33	<b>1128<math>\pm</math>3.67</b>
Domain-Incremental	Digit10 (Task:4)	410 $\pm$ 1.67	412 $\pm$ 0.67	112 $\pm$ 0.33	483 $\pm$ 1.33	372 $\pm$ 2.00	410 $\pm$ 1.67	419 $\pm$ 2.67	<b>325<math>\pm</math>1.33</b>
	Office31 (Task:3)	413 $\pm$ 2.67	429 $\pm$ 2.00	144 $\pm$ 0.67	436 $\pm$ 3.67	391 $\pm$ 1.12	413 $\pm$ 2.67	431 $\pm$ 3.33	<b>388<math>\pm</math>1.67</b>
	DomainNet (Task:6)	726 $\pm$ 3.33	767 $\pm$ 2.67	141 $\pm$ 1.67	752 $\pm$ 4.00	694 $\pm$ 2.67	726 $\pm$ 3.33	791 $\pm$ 3.67	<b>661<math>\pm</math>2.33</b>

# Experiments - Performance Overview

## Data Heterogeneity



a smaller  $\alpha$  indicates higher data heterogeneity

$$v_{k,s}^{t-1} = v_{k,s-1}^{t-1} - \eta \left( \sum_{i=1}^M \nabla l \left( f_{v_{k,s-1}^{t-1}}(\tilde{x}_{k,t-1}^{(i)}), \tilde{y}_{k,t-1}^{(i)} \right) + q(\lambda)(v_{k,s-1}^{t-1} - w^{t-1}) \right). \quad (3)$$

Dataset	$\alpha = 0.1$			$\alpha = 0.5$			$\alpha = 1.0$			$\alpha = 10$		
	$\lambda = 0.2$	$\lambda = 0.5$	$\lambda = 0.8$	$\lambda = 0.2$	$\lambda = 0.5$	$\lambda = 0.8$	$\lambda = 0.2$	$\lambda = 0.5$	$\lambda = 0.8$	$\lambda = 0.2$	$\lambda = 0.5$	$\lambda = 0.8$
CIFAR10	<b>18.75<math>\pm</math>1.30</b>	18.61 $\pm$ 1.09	17.91 $\pm$ 0.81	<b>26.25<math>\pm</math>1.64</b>	26.00 $\pm$ 0.97	25.62 $\pm$ 0.52	27.05 $\pm$ 0.88	27.80 $\pm$ 0.21	<b>29.22<math>\pm</math>0.49</b>	38.43 $\pm$ 0.43	40.04 $\pm$ 0.19	<b>42.17<math>\pm</math>0.25</b>
Office31	<b>41.25<math>\pm</math>1.01</b>	39.29 $\pm$ 1.34	38.18 $\pm$ 0.68	46.86 $\pm$ 0.91	<b>47.64<math>\pm</math>0.53</b>	47.13 $\pm$ 1.16	43.81 $\pm$ 0.73	48.67 $\pm$ 0.99	<b>50.08<math>\pm</math>0.77</b>	52.79 $\pm$ 1.28	55.92 $\pm$ 0.38	<b>58.51<math>\pm</math>0.46</b>
Tiny-ImageNet	<b>22.32<math>\pm</math>0.12</b>	20.51 $\pm$ 0.98	18.00 $\pm$ 1.30	24.60 $\pm$ 0.48	<b>25.42<math>\pm</math>0.59</b>	24.39 $\pm$ 0.66	24.88 $\pm$ 0.87	27.15 $\pm$ 0.78	<b>27.84<math>\pm</math>0.73</b>	29.03 $\pm$ 0.30	30.26 $\pm$ 0.24	<b>32.07<math>\pm</math>0.27</b>

# Conclusions

We propose a simple framework called **Re-Fed** to address the issues of catastrophic forgetting and data heterogeneity in federated continual learning. It has the following advantages:

- ✓ **Optimization**: Re-Fed allows for the use of aggregation methods other than FedAvg to update the global model while maintaining convergence properties.
- ✓ **Privacy**: Unlike typical FL algorithms, Re-Fed does not transmit additional information over the network, thus avoiding privacy issues that arise from applying sample reconstruction methods for data replay.
- ✓ **Resources**: Re-Fed enables each client to train a base model using only its local training data without requiring additional distilled or generated augmented data, thereby avoiding extra computational costs or storage overhead.



# Thank You

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